

緒論部分

[0-1] 解: 令 CO_2 為 A, H_2O 為 B, 依題意知:

$$n_A = 0.05 \text{ kmol} = 50 \text{ mol}$$

$$m_B = 1000 \text{ kg} \quad M_B = 18 \text{ kg/kmol}$$

$$\therefore n_B = \frac{m_B}{M_B} = \frac{1000}{18} = 55.55 \text{ kmol} = 55.55 \times 10^3 \text{ mol}$$

故溶液中 CO_2 的摩尔分數為:

$$x_A = \frac{n_A}{n_A + n_B} = \frac{50}{50 + 55.55 \times 10^3} = 0.0009$$

[0-2] 解: 由附表可查得甲醇的安托因常數為:

$$A = 7.19736 \quad B = 1574.99 \quad C = 238.86$$

$$\text{据 } \lg P^0 = A - \frac{B}{t + C}$$

$$\text{已知 } t = 25^\circ\text{C}$$

$$\therefore \lg P^0 = 7.19736 - \frac{1574.99}{25 + 238.86} = 1.2283$$

故甲醇的飽和蒸氣壓為:

$$P^s = P^0 = 16.92 \text{ kPa}$$

$$\therefore y_A = \frac{n_A}{n} = \frac{P_A}{P}$$



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已知 $P_A = 16.92 \times 10^3 \text{ Pa}$ $P = 101325 \text{ Pa}$

$$\therefore y_A = \frac{16.92 \times 10^3}{101325} = 0.167$$

据 $w_A = \frac{y_A M_A}{y_A M_A + y_B M_B}$

已知 $M_A = 32$ $M_B = 29$ $y_B = 1 - 0.167 = 0.833$

$$\therefore w_A = \frac{0.167 \times 32}{0.167 \times 32 + 0.833 \times 29} = 0.181$$

由 $P_A V = n_A R T$

故 $C_A = \frac{n_A}{V} = \frac{P_A}{R T}$

已知 $P_A = 16.92 \times 10^3 \text{ Pa}$ $T = 273 + 25 = 298 \text{ K}$

$$\therefore C_A = \frac{16.92 \times 10^3}{8.314 \times 298} = 6.83 \text{ (mol/m}^3\text{)} = 6.83 \times 10^{-3} \text{ (kmol/m}^3\text{)}$$

据 $P_A = C_A M_A$

$$\therefore P_A = 6.83 \times 10^{-3} \times 32 = 0.22 \text{ (kg/m}^3\text{)}$$

[0-3] 解: 令 NaOH 为组分 1, NaCl 为组分 2, H₂O 为组分 3。

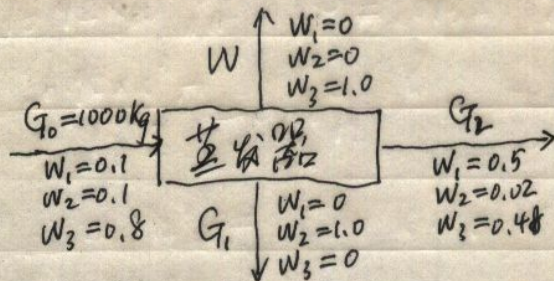
画一个草图将过程示意出来, 如图所示。

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绪论

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列出各种物料衡算式如下:

总物料: $1000 = W + G_1 + G_2$ ----- (1)

NaCl: $1000 \times 0.1 = 1 \times G_1 + 0.02 G_2$ ----- (2)

NaOH: $1000 \times 0.1 = 0.5 G_2$ (关键组分) ----- (3)

由(3)式可求得食盐分离后的浓缩液量为:

$$G_2 = 200 \text{ Kg}$$

将 G_2 代入(2)式可求得分离的食盐量:

$$G_1 = 96 \text{ Kg}$$

将 G_1, G_2 代入(1)式可求得水分量:

$$W = 704 \text{ Kg}$$

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1-6 例：如右圖所示，在 U 型壓差計兩側出口所處的截面之間進行能量衡算，運用柏努利方程，係注意點：

$$Z_1 = Z_2 = 0 \quad (\text{取管路的軸線為基準面})$$

$$H_e = 0 \quad (\text{無外加能量})$$

$$\text{據 } Q_v = \frac{\pi}{4} d^2 u$$

$$\text{且知 } d_1 = 0.04 \text{ m} \quad d_2 = 0.08 \text{ m} \quad Q_v = 2.78 \times 10^{-3} \text{ m}^3/\text{s}$$

$$\text{故 } u_1 = \frac{4Q_v}{\pi d_1^2} = \frac{4 \times 2.78 \times 10^{-3}}{3.14 \times 0.04^2} = 2.2 \text{ m/s}$$

$$u_2 = \frac{4Q_v}{\pi d_2^2} = \frac{4 \times 2.78 \times 10^{-3}}{3.14 \times 0.08^2} = 0.55 \text{ m/s}$$

$$\text{據 } \Delta p = p_1 - p_2 = (p_A - p_B) g R$$

$$\text{已知 } p_A = 1600 \text{ kg/m}^3 \quad p_B = 1000 \text{ kg/m}^3 \quad R = -0.165 \text{ m}$$

$$\therefore p_1 - p_2 = (1600 - 1000) \times 9.81 \times (-0.165) \\ = -971.2 \text{ Pa}$$

$$\text{據 } Z_1 + \frac{u_1^2}{2g} + \frac{p_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{p_2}{\rho g} + H_f$$

$$\therefore H_f = \frac{u_1^2 - u_2^2}{2g} + \frac{p_1 - p_2}{\rho g} \\ = \frac{2.2^2 - 0.55^2}{2 \times 9.81} - \frac{971.2}{1000 \times 9.81} = 0.132 \text{ (m)}$$

$$\text{據 } H_f = \xi \frac{u^2}{2g}$$



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由此可求得局部阻力係數為：

$$\xi = \frac{2gH_f}{u^2} = \frac{2 \times 9.81 \times 0.132}{2.2^2} = 0.536$$

1-6 段：由於兩截面間連接了一個倒置 U 型管壓差計，故：

$$\Delta p = (p_A - p_B) g R$$

依題意知， $p_A = 1000 \text{ kg/m}^3$ ， $p_B = 1.25 \text{ kg/m}^3$ (空氣)

$$R = 0.1 \text{ m}$$

故兩截面間的压强差為：

$$\Delta p = (1000 - 1.25) \times 9.81 \times 0.1 = 9810 \text{ Pa}$$

在兩截面間運用柏努利方程，以管路軸線為基準面，依題意知， $Z_1 = Z_2 = 0$ ， $q_m = 3 \text{ kg/s}$

$$d_1 = 0.036 \text{ m}, d_2 = 0.053 \text{ m}, \rho = 1000 \text{ kg/m}^3$$

$$q_v = \frac{q_m}{\rho} = \frac{3}{1000} = 3 \times 10^{-3} \text{ (m}^3/\text{s)}$$

$$u_1 = \frac{4q_v}{\pi d_1^2} = \frac{4 \times 3 \times 10^{-3}}{3.14 \times 0.036^2} = 2.95 \text{ (m/s)}$$

$$u_2 = \frac{4q_v}{\pi d_2^2} = \frac{4 \times 3 \times 10^{-3}}{3.14 \times 0.053^2} = 1.36 \text{ (m/s)}$$

$$\text{根據 } Z_1 + \frac{u_1^2}{2g} + \frac{p_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{p_2}{\rho g} + H_f$$



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$$\therefore H_f = \frac{P_1 - P_2}{\rho g} + \frac{u_1^2 - u_2^2}{2g}$$

$$= \frac{981}{1000 \times 9.81} + \frac{2.95^2 - 1.36^2}{2 \times 9.81} = 0.45$$

$$\text{据 } H_f = \frac{\Delta P_f}{\rho g}$$

故知两截面间的压强降为:

$$\Delta P_f = \rho g H_f = 1000 \times 9.81 \times 0.45 = 4.41 \times 10^3 \text{ (Pa)}$$

1-7解: (1) 设贮水槽水面距放水管轴线之高度为 Z , 依题意有: $Z + h = \frac{\rho_{Hg}}{\rho} R$

$$\text{已知 } h = 1.51 \text{ m } R = 0.62 \text{ m } \rho = 1000 \text{ kg/m}^3$$

$$\text{可求得: } Z = 6.922 \text{ m}$$

当闸阀都打开时, 在贮水槽水面与 U 型水银压差计所对应的左侧放水管截面之间运用柏努利方程, 并以放水管轴线为基准面, 依题意有:

$$Z_1 = 6.922 \text{ m } Z_2 = 0 \quad u_1 \approx 0 \quad u_2 = u \quad P_1 = P_a \quad H_e = 0$$

$$P_2 + \rho g h' = \rho_{Hg} g R' + P_a$$

$$\text{已知 } h' = 1.41 \text{ m } R' = 0.42 \text{ m}$$

$$\therefore P_2 = P_a + 13600 \times 9.81 \times 0.42 - 1000 \times 9.81 \times 1.41 = P_a + 42202.62$$



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$$H_f = \left(\lambda \frac{L}{d} + \xi \right) \frac{u^2}{2g}$$

已知: $\lambda = 0.02$ $L = 15 \text{ m}$ $d = 0.1 \text{ m}$ $\xi = 0.5$

$$\therefore H_f = \left(0.02 \times \frac{15}{0.1} + 0.5 \right) \frac{u^2}{2g} = 0.1784 u^2$$

据 $Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$

$$6.922 + \frac{P_a}{\rho g} = \frac{u^2}{2g} + \frac{P_a + 42202.62}{\rho g} + 0.1784 u^2$$

解得: $u = 3.38 \text{ m/s}$

故水的流量为:

$$Q_v = \frac{\pi}{4} d^2 u = \frac{\pi}{4} \times 0.1^2 \times 3.38$$

$$= 0.02653 \text{ m}^3/\text{s} = 95.5 \text{ m}^3/\text{h}$$

(2) 当闸阀全开时, 在贮水槽水面与放水管道出口之间运用柏努利方程, 以放水管道轴线为基准面, 依题意有:

$$Z_1 = 6.922 \text{ m} \quad Z_2 = 0 \quad u_1 = 0 \quad u_2 = u$$

$$P_1 = P_2 = P_a \quad H_e = 0$$

$$H_f = \left[\lambda \left(\frac{L}{d} + \frac{L_e}{d} \right) + \xi \right] \frac{u^2}{2g}$$

已知: $\lambda = 0.018$ $L = 35 \text{ m}$ $\frac{L_e}{d} = 15$ $\xi = 0.5$



$$\therefore H_f = \left[0.018 \times \left(\frac{35}{0.1} + 15 \right) + 0.5 \right] \frac{u^2}{2g} = 0.36u^2$$

据 $Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$

$$\therefore 6.922 = \frac{u^2}{2g} + 0.36u^2$$

解得: $u = 4.1 \text{ m/s}$

再在短水槽水面与喷嘴口所对应的截面之间应用柏努利方程, 以短水槽水面为基准面。依题意有:

$$Z_1 = 6.922 \text{ m} \quad Z_2 = 0 \quad u_1 \approx 0 \quad u_2 = 4.1 \text{ m/s} \quad P_1 = P_a \quad P_2 = P_2$$

$$H_e = 0$$

$$H_f = \left(\lambda \frac{L}{d} + \xi \right) \frac{u_2^2}{2g}$$

且已知 $\lambda = 0.018 \quad \xi = 0.5$

$$\therefore H_f = \left(0.018 \times \frac{15}{0.1} + 0.5 \right) \times \frac{4.1^2}{2 \times 9.81} = 2.742 \text{ (m)}$$

据 $Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$

$$\therefore 6.922 + \frac{P_a}{\rho g} = \frac{4.1^2}{2 \times 9.81} + \frac{P_2}{\rho g} + 2.742$$

解得: $P_2 = P_a + 32603.82$



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由(1)知 U 型水银压差计内 $R=0$ 时, 其水柱高度:

$$h(0) = 1.51 - \frac{0.62}{2} = 1.2 \text{ (m)}$$

设 U 型管压差计读数为 R , 则水柱高度应为

$$h = 1.2 + \frac{R}{2}$$

依题意有:

$$P_a + 32603.82 + (1.2 + \frac{R}{2}) \times 1000 \times 9.81 = P_a + 13600 \times 9.81 R$$

由此可解得 U 型管压差计读数:

$$R = 0.345 \text{ m}$$

1-8 解(1) 已知 q_v, l 不变

$$\text{据 } \Delta P_f = \lambda \frac{l}{d} \frac{\rho u^2}{2}$$

当流体在管内为层流时: $\lambda = \frac{64}{Re}$

$$\text{则 } \lambda = \frac{64}{Re} = \frac{64}{\frac{d u \rho}{\mu}} = \frac{64}{\frac{4 d q_v \rho}{\mu \pi d^2}} = \frac{64 \pi \mu d}{4 q_v \rho} \propto d$$

$$u = \frac{4 q_v}{\pi d^2} \propto \frac{1}{d^2}$$

$$\therefore \Delta P_f = \lambda \frac{l}{d} \frac{\rho u^2}{2} \propto \frac{1}{d^4}$$



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当 $d' = 1.3d$ 时

$$\frac{\Delta P_f'}{\Delta P_f} = \frac{d^4}{d'^4} = \frac{d^4}{(1.3d)^4} = \left(\frac{1}{1.3}\right)^4 = 0.35$$

(2) 当流体在光滑管内为湍流, 且 $Re = 10^5$ 时,

$$\lambda = \frac{0.3164}{Re^{0.25}}$$

$$\therefore \lambda \propto d^{0.25}$$

$$\text{故 } \Delta P_f \propto d^{0.25} \times \frac{1}{d} \times \frac{1}{d^4} = \frac{1}{d^{4.75}}$$

当 $d' = 1.3d$ 时

$$\frac{\Delta P_f'}{\Delta P_f} = \left(\frac{1}{1.3}\right)^{4.75} = 0.288$$

(3) 当管内流动处于阻力平方区, $\lambda = 0.11\left(\frac{\epsilon}{d}\right)^{0.25}$ 时,

$$\lambda \propto \left(\frac{1}{d}\right)^{0.25}$$

$$\text{故 } \Delta P_f \propto \left(\frac{1}{d}\right)^{0.25} \times \frac{1}{d} \times \frac{1}{d^4} = \frac{1}{d^{5.25}}$$

当 $d' = 1.3d$ 时

$$\frac{\Delta P_f'}{\Delta P_f} = \left(\frac{1}{1.3}\right)^{5.25} = 0.252$$



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1-9 解：依題意知操作條件下空氣的體積流量為：

$$Q_v = \frac{\pi}{4} d^2 u n$$

$$\text{已知 } d = 0.02 \text{ m} \quad u = 9 \text{ m/s} \quad n = 13$$

$$\therefore Q_v = \frac{\pi}{4} \times 0.02^2 \times 9 \times 13 = 0.0368 \text{ m}^3/\text{s}$$

$$\therefore Q_m = \rho_m Q_v$$

$$\text{而 } \rho_m = \rho_0 \cdot \frac{P}{P_0} \cdot \frac{T_0}{T}$$

$$\text{已知 } \rho_0 = 1.293 \text{ kg/m}^3 \quad T = 323 \text{ K} \quad P = 1.96 \times 10^5 + 9.87 \times 10^4 = 2.947 \times 10^5 \text{ Pa}$$

$$\therefore \rho_m = 1.293 \times \frac{2.947 \times 10^5}{101325} \times \frac{273}{323} = 3.18 \text{ kg/m}^3$$

故空氣的質量流量為：

$$Q_m = 3.18 \times 0.0368 = 0.117 \text{ kg/s}$$

$$\therefore Q_v = Q_{v0} \cdot \frac{P_0}{P} \cdot \frac{T}{T_0}$$

故標準狀況下的體積流量為：

$$Q_{v0} = Q_v \cdot \frac{P}{P_0} \cdot \frac{T_0}{T} = 0.0368 \times \frac{2.947 \times 10^5}{101325} \times \frac{273}{323}$$

$$= 0.0905 \text{ (m}^3/\text{s)}$$



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1-10分: 已知 $d=0.015\text{ m}$ $u=0.6\text{ m/s}$ $\rho=830\text{ kg/m}^3$
 $\mu=5\times 10^{-3}\text{ Pa}\cdot\text{s}$

$$\therefore (1) Re = \frac{du\rho}{\mu} = \frac{0.015 \times 0.6 \times 830}{5 \times 10^{-3}} = 1494$$

(2) 由 $Re=1494$ 可知管内流动为层流, 据:

$$u = u_{\max} \left(1 - \frac{r^2}{R^2}\right)$$

$$\text{且 } u = \bar{u}$$

$$\text{而 } \bar{u} = \frac{1}{2} u_{\max}$$

$$\therefore 1 - \frac{r^2}{R^2} = \frac{1}{2}$$

$$\text{已知 } R = \frac{d}{2} = \frac{0.015}{2}$$

$$\text{可得: } r = 0.0053\text{ m} = 5.3\text{ mm}$$

(3) 层流流动时:

$$\lambda = \frac{64}{Re} = \frac{64}{1494} = 0.043$$

$$\text{据 } \Delta P_f = \lambda \frac{L}{d} \frac{\rho u^2}{2}$$

$$\text{已知 } L = 15\text{ m}$$

$$\therefore \Delta P_f = 0.043 \times \frac{15}{0.015} \times \frac{830 \times 0.6^2}{2} = 6400\text{ (Pa)}$$



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1-11 解：在 A、B 兩截面之間列柏努利方程，已知：

$$Z_1 \approx Z_2, u_1 = u_2, H_e = 0, \Delta h = 0.45 \text{ m}, d = 0.05 \text{ m}.$$

依題意知：

$$P_1 - P_2 = \rho g \Delta h$$

$$\text{根據 } Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$$

故 A、B 段總阻力損失為：

$$H_f = \frac{P_1 - P_2}{\rho g} = \Delta h = 0.45 \text{ (m)}$$

其中直管阻力損失為 H_{f1} ，已知 $Q_v = 0.0023 \text{ m}^3/\text{s}$ ，故管內流速：

$$u = \frac{4Q_v}{\pi d^2} = \frac{4 \times 0.0023}{3.14 \times 0.05^2} = 1.17 \text{ (m/s)}$$

$$\text{根據 } H_{f1} = \lambda \frac{L}{d} \frac{u^2}{2g}$$

$$\text{已知 } \lambda = 0.03, L = 10 \text{ m}$$

$$\therefore H_{f1} = 0.03 \times \frac{10}{0.05} \times \frac{1.17^2}{2 \times 9.81} = 0.42 \text{ (m)}$$

由此可知局部阻力 H_{f2} 為：

$$H_{f2} = H_f - H_{f1} = 0.45 - 0.42 = 0.03 \text{ (m)}$$

$$\text{根據 } H_{f2} = \zeta \frac{u^2}{2g}$$

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$$\frac{P_2 - P_1}{\rho g} = 2.98 \text{ (m)}$$

$$\text{或 } P_2 = P_1 + 2.98 \rho g = P_1 + 29236.8$$

對於 U 型管內 P_A 與 P_B 有：

$$P_A = P_2$$

$$P_B = P_1 + \rho g h = P_1 + 1000 \times 9.81 \times 1.5 = P_1 + 14715$$

$$\therefore P_A - P_B = P_2 - P_1 - \rho g h$$

$$= P_1 + 29236.8 - P_1 - 14715 = 14521.8 \text{ (Pa)} > 0$$

故知左側壓强大於右側，因而右側的水銀面高。

設壓差計的讀數為 R ，則：

$$\Delta P = P_A - P_B = (\rho_0 - \rho) g R$$

$$\therefore R = \frac{P_A - P_B}{(\rho_0 - \rho) g} = \frac{14521.8}{(13600 - 1000) \times 9.81} = 0.117 \text{ (m)}$$

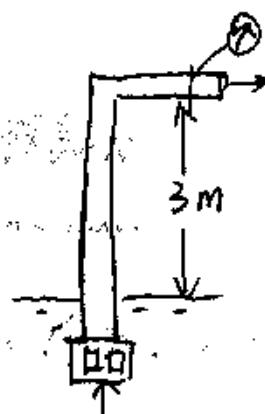
1-13 解：如圖所示：

$$\text{已知 } Q_v = 0.005 \text{ m}^3/\text{s}, d = 0.05 \text{ m}$$

$$\therefore u = \frac{4 Q_v}{\pi d^2} = \frac{4 \times 0.005}{3.14 \times 0.05^2} = 2.55 \text{ (m/s)}$$

$$\therefore Re = \frac{d u \rho}{\mu} = \frac{0.05 \times 2.55 \times 998}{1.005 \times 10^{-3}}$$

$$= 1.27 \times 10^5$$



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且 $\varepsilon/d = \frac{0.12}{150} = 0.004$

由摩擦系数图, 可得 $\lambda = 0.0295$

吸入管总阻力损失为:

$$H_f = (\lambda \frac{l}{d} + \zeta_1 + \zeta_2) \frac{u^2}{2g}$$

$$= (0.0295 \times \frac{8}{0.05} + 10 + 0.75) \times \frac{2.55^2}{2 \times 9.81} = 5.127 \text{ (m)}$$

在吸入端液面与真空表所处截面间列柏努利方程,
以吸入端液面为基准面, 依题意知:

$$Z_1 = 0, Z_2 = 3 \text{ m}, u_1 \approx 0, u_2 = 2.55 \text{ m/s}, P_1 = P_a$$

$$P_2 = P, H_e = 0, H_f = 5.127 \text{ m}$$

据: $Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$

$$\therefore \frac{P_a}{\rho g} = 3 + \frac{2.55^2}{2 \times 9.81} + \frac{P}{\rho g} + 5.127$$

解得 $P = P_a - 8281.2$

由此可知吸入口水银压差计真空表的读数为:

$$h = \frac{P}{\rho_{\text{Hg}} g} = \frac{8281.2}{13600 \times 9.81} = 0.62 \text{ mHg} = 620 \text{ (mm)}$$

为增大输水量, 则入口处的动压头增大, 管沿阻力增大,
故真空表的读数亦增大。



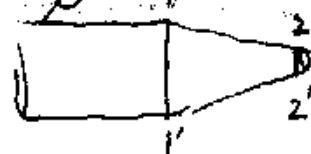
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1-14 解：如圖所示，在 1、2 截面之間列柏努利方程，以管路軸線為基準面，依題意

$$\text{知： } Z_1 = Z_2 \quad H_e = 0$$

$$H_f \approx 0 \quad P_1 = P_a + 0.8 \times 10^6$$

$$Q_v = 0.025 \text{ m}^3/\text{s} \quad d_1 = 0.08 \text{ m} \quad d_2 = 0.04 \text{ m} \quad P_2 = P$$



$$\text{則： } u_1 = \frac{4 \times 0.025}{3.14 \times 0.08^2} = 4.98 \text{ m/s}$$

$$u_2 = \frac{4 \times 0.025}{3.14 \times 0.04^2} = 19.9 \text{ m/s}$$

$$\text{據 } Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$$

$$\therefore \frac{4.98^2}{2 \times 9.81} + \frac{P_a + 0.8 \times 10^6}{1000 \times 9.81} = \frac{19.9^2}{2 \times 9.81} + \frac{P}{1000 \times 9.81}$$

$$\text{解得： } P = P_a + 614400$$

水進入噴嘴時壓力（與流體流動方向相同）為：

$$F_1 = P_1 A_1 = (101325 + 0.8 \times 10^6) \times \frac{\pi}{4} \times 0.08^2 = 4528.2 \text{ (N)}$$

水離開噴嘴時的壓力（與流動方向相反）為：

$$F_2 = P_2 A_2 = (101325 + 614400) \times \frac{\pi}{4} \times 0.04^2 = 898.95 \text{ (N)}$$

由此可知水流對噴嘴的淨作用力為：

$$F = F_1 - F_2 = 4528.2 - 898.95$$

$$= 3629 \text{ (N)}$$



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1-15 7A. (1) 按假設截面 A 點的水通過循環系統管路
元素能回到截面 A 處, 則水經過管路的能量損失
即為系所提供的能量, 即:

$$W_e = \sum h_{f1} + \sum h_{f2}$$

$$\text{已知 } \sum h_{f1} = 98.1 \text{ J/Kg} \quad \sum h_{f2} = 49 \text{ J/Kg}$$

$$\therefore W_e = 98.1 + 49 = 147.1 \text{ J/Kg}$$

$$\text{據 } N_e = q_v \rho W_e$$

$$\text{已知 } q_v = 0.0125 \text{ m}^3/\text{s} \quad \rho = 1100 \text{ Kg/m}^3 \quad \eta = 70\%$$

$$\therefore N_e = 0.0125 \times 1100 \times 147.1 = 2023 \text{ (W)}$$

故泵的軸功率為:

$$N = \frac{N_e}{\eta} = \frac{2023}{0.7} = 2889 \text{ (W)} = 2.89 \text{ (KW)}$$

(2) 在換熱器一側 A、B 兩压力表裝口所處截面之間列
柏努利方程, 并以 A 點為基準面, 依題意有:

$$Z_1 = 0 \quad Z_2 = 7 \text{ m} \quad u_1 = u_2 \quad P_1 = P_a + 2.5 \times 10^5 \quad P_2 = P_B$$

$$W_e = 0 \quad \sum h_f = 98.1 \text{ J/Kg}$$

$$\text{據: } Z_1 g + \frac{u_1^2}{2} + \frac{P_1}{\rho} + W_e = Z_2 g + \frac{u_2^2}{2} + \frac{P_2}{\rho} + \sum h_f$$

$$\therefore \frac{P_a + 2.5 \times 10^5}{1100} = 7 \times 9.81 + \frac{P_B}{1100} + 98.1$$

$$\text{解得: } P_B = P_a + 66553 = 66553 \text{ Pa (表壓)}$$



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1-16 解：首先在吸入端液面與吸入管路中某入口處真實表所截截面列伯努利方程，以吸入端液面為基準面，依題意已知： $Z_1 = 0$ $Z_2 = 1.5 \text{ m}$ $P_1 = P_a$ $P_2 = P_a - 2.47 \times 10^4$
 $u_1 \approx 0$ $u_2 = u$ $W_e = 0$ $\Sigma h_f = 2u^2$

$$\text{据 } Z_1 g + \frac{u_1^2}{2} + \frac{P_1}{\rho} + W_e = Z_2 g + \frac{u_2^2}{2} + \frac{P_2}{\rho} + \Sigma h_f$$

$$\therefore \frac{P_a}{1000} = 1.5 \times 9.81 + \frac{u^2}{2} + \frac{P_a - 2.47 \times 10^4}{1000} + 2u^2$$

$$\text{解得： } u = 2 \text{ m/s}$$

然后在貯液槽液面與排水管與噴頭連接處列伯努利方程，以貯液槽液面為基準面，依題意已知：

$$Z_1 = 0$$

$$Z_2 = 14 \text{ m}$$

$$u_1 \approx 0$$

$$u_2 = 2 \text{ m/s}$$

$$P_1 = P_a$$

$$P_2 = P_a + 9.5 \times 10^4$$

$$W_e = W_e$$

$$\Sigma h_f = \Sigma h_{f1} + \Sigma h_{f2} = 12u^2$$

$$\text{据 } Z_1 g + \frac{u_1^2}{2} + \frac{P_1}{\rho} + W_e = Z_2 g + \frac{u_2^2}{2} + \frac{P_2}{\rho} + \Sigma h_f$$

$$\therefore \frac{P_a}{1000} + W_e = 14 \times 9.81 + \frac{2^2}{2} + \frac{P_a + 9.5 \times 10^4}{1000} + 12 \times 2^2$$

$$\text{解得： } W_e = 282.34 \text{ (J/kg)}$$

$$Q_v = \frac{\pi}{4} d^2 u = \frac{\pi}{4} \times 0.071^2 \times 2 = 0.0079 \text{ (m}^3/\text{s)}$$

故系統有效功率為

$$N_e = Q_v \rho W_e = 0.0079 \times 1000 \times 282.34 = 2.23 \text{ (kW)}$$



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1-17 解：对于烟囱内的烟气流，已知 $d=2\text{m}$, $q_v=22.2\text{m}^3/\text{s}$

$$\therefore u = \frac{4q_v}{\pi d^2} = \frac{4 \times 22.2}{3.14 \times 2^2} = 7.07 \text{ (m/s)}$$

已知 $\rho=0.67\text{Kg/m}^3$ $\mu=2.6 \times 10^{-5}\text{Pa}\cdot\text{s}$

$$\therefore Re = \frac{du\rho}{\mu} = \frac{2 \times 7.07 \times 0.67}{2.6 \times 10^{-5}} = 3.64 \times 10^5$$

已知 $\varepsilon/d=0.0004$

根据雷诺摩擦系数图可知 $\lambda=0.0177$

故烟囱内的流动阻力损失 (不包括出口损失) 为

$$H_f = \lambda \frac{H}{d} \frac{u^2}{2g} = 0.0177 \times \frac{H}{2} + \frac{7.07^2}{2 \times 9.81} = 0.023H$$

烟囱外的大气视为静止状态，地面处压强为 P_a ，烟囱顶部处压强为 P_2 。已知 $\rho_a=1.15\text{Kg/m}^3$ ，根据静力学原理：

$$P_a = P_2 + \rho_a g H$$

$$= P_2 + 1.15 \times 9.81 H = P_2 + 11.28 H$$

在烟囱内底部至烟囱出口内侧面之间列柏努利方程，以烟囱内底部为基准面，依题意有：

$$Z_1=0 \quad Z_2=H \quad u_1=u_2 \quad P_1=P_a-196 \quad P_2=P_a-11.28H$$

$$H_e=0 \quad H_f=0.023H$$

$$\text{据 } Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$$

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$$\therefore \frac{P_a - 196}{0.67 \times 9.81} = H + \frac{P_a - 11.28H}{0.67 \times 9.81} + 0.023H$$

由此可求得烟囱的高度: $H = 43 \text{ m}$ 。

1-18 解: 依题意知 ab 管段 $d = 0.01 \text{ m}$ $\rho = 0.5 \text{ kg/m}^3$
 $\mu = 2 \times 10^{-5} \text{ Pa} \cdot \text{s}$ 设管内流速为 u 。

$$\text{则 } Re = \frac{d u \rho}{\mu} = \frac{0.01 \times u \times 0.5}{2 \times 10^{-5}} = 250 u$$

考虑到气体粘度、管径均很小, 设流体在管内的流动型态为层流, 则:

$$\lambda = \frac{64}{Re} = \frac{64}{250 u}$$

由此可知气体通过 ab 管段的阻力损失为:

$$H_f = \lambda \frac{le}{d} \frac{u^2}{2g}$$

已知 $le = 10 \text{ m}$

$$\therefore H_f = \frac{64}{250 u} \times \frac{10}{0.01} \times \frac{u^2}{2 \times 9.81} = 13.05 u$$

在 a, b 管段之间列柏努利方程, 以入口 a 为基准面。
 依题意知: $Z_1 = 0$ $Z_2 \approx 0$ (忽略) $u_1 = u_2 = u$

$$P_1 = P_2 = P - \rho_m g H \quad H = 0.042 \quad H_e = 0$$



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$$\text{据 } Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$$

$$\therefore \frac{P}{0.5 \times 9.81} = \frac{P - 1000 \times 9.81 \times 0.042}{0.5 \times 9.81} + 13.05 u$$

$$\text{解得: } u = 6.44 \text{ m/s}$$

故气体通过ab段的流量为:

$$Q_v = \frac{\pi}{4} d^2 u = \frac{\pi}{4} \times 0.01^2 \times 6.44 = 5.05 \times 10^{-4} (\text{m}^3/\text{s}) = 1.82 \text{ m}^3/\text{h}$$

$$\therefore Re = \frac{du\rho}{\mu} = \frac{0.01 \times 6.44 \times 0.5}{2 \times 10^{-5}} = 1610 < 2000$$

故假设成立, 计算结果有效。

1-19 解: 在如图所系的a、o截面间列柏努利方程, 以管路的轴线为基准面, 依题意知:

$$Z_1 = Z_2 \quad u_1 = u_2 \quad u_2 = u_2 \quad H_e = 0$$

$$P_1 - P_2 = (P_{Hg} - P_{mo}) g R = (13600 - 1000) \times 9.81 \times 0.3 = 37081.8 \text{ Pa}$$

$$H_f = 3 \frac{u_2^2}{2g} = 0.15 \frac{u_2^2}{2g}$$

$$\text{据 } Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$$

$$\therefore \frac{u_1^2}{2g} + \frac{P_1}{\rho g} = \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + 0.15 \frac{u_2^2}{2g}$$



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代入数据并化简后所得:

$$0.575 u_2^2 - 0.5 u_1^2 = 37.082 \quad \dots\dots (1)$$

$$\text{又: } \frac{u_2}{u_1} = \left(\frac{d_1}{d_2}\right)^2 = \left(\frac{0.1}{0.05}\right)^2 = 4$$

$$\therefore u_2 = 4u_1 \quad \dots\dots (2)$$

联立(1)、(2)两式可解得: $u_1 = 2.06 \text{ m/s}$

由此可求得管道的输水量为:

$$\begin{aligned} q_v &= \frac{\pi}{4} d_1^2 u_1 = \frac{\pi}{4} \times 0.1^2 \times 2.06 \\ &= 0.0162 \text{ (m}^3/\text{s)} = 58.34 \text{ (m}^3/\text{h)} \end{aligned}$$

1-207解: 据转子流量计的计算公式:

$$q_v = C_R A_2 \sqrt{\frac{2gV_f(P_f - P)}{A_f P}}$$

当转子的形状及大小均不改变时, 仅改变其材质(P), 则流量的关系有:

$$\frac{q'_v}{q_v} = \sqrt{\frac{P'_f - P}{P_f - P}}$$

$$\text{已知: } P'_f = 10670 \text{ Kg/m}^3 \quad P_f = 7920 \text{ Kg/m}^3 \quad P = 1000 \text{ Kg/m}^3$$

$$\therefore \frac{q'_v}{q_v} = \sqrt{\frac{10670 - 1000}{7920 - 1000}} = 1.182$$



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由此可知：若原测量范围为 $0.250 \sim 2.50 \text{ m}^3/\text{h}$ ，则更换转子后的测量范围为 $0.296 \sim 2.96 \text{ m}^3/\text{h}$ 。

若同来测量乙醇 ($\rho_2 = 789 \text{ kg/m}^3$)：

$$\text{据 } \frac{q_{v,2}}{q_{v,1}} = \sqrt{\frac{\rho_1(\rho_f - \rho_2)}{\rho_2(\rho_f - \rho_1)}}$$

$$\text{已知： } \rho_1 = 1000 \text{ kg/m}^3 \quad \rho_f = 10670 \text{ kg/m}^3 \quad \rho_2 = 789 \text{ kg/m}^3$$

$$\therefore \frac{q_{v,2}}{q_{v,1}} = \sqrt{\frac{1000 \times (10670 - 789)}{789 \times (10670 - 1000)}} = 1.138$$

$$\therefore q_{v,1} = 0.296 \sim 2.96 \text{ m}^3/\text{h}$$

故知测量乙醇时的流量范围为：

$$q_{v,2} = 1.138 q_{v,1} = 1.138 \times (0.296 \sim 2.96)$$

$$= 0.337 \sim 3.37 (\text{m}^3/\text{h})$$

1-24 解：由于使用的是微差计，故流速的计算式为：

$$u = \sqrt{\frac{2Rg(\rho_k - \rho_{油})}{\rho_k}}$$

$$\text{已知： } \rho_k = 998 \text{ kg/m}^3 \quad \rho_{油} = 835 \text{ kg/m}^3 \quad R = 0.08 \text{ m}$$

$$\text{据 } \rho_k = \frac{PM}{RT}$$

$$\text{已知 } P = 98.66 \times 10^3 - 490 \quad T = 293 \quad M = 29 \times 10^{-3}$$

$$\therefore \rho_k = 1.17 \text{ kg/m}^3$$



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故空氣在管中心處的流速為：

$$u = \sqrt{\frac{2 \times 0.08 \times 9.81 \times (998 - 835)}{1.17}} = 14.8 \text{ (m/s)}$$

1-22 解：當流體在圓管內作層流流動時：

$$u = u_{\max} \left(1 - \frac{r^2}{R^2}\right)$$

$$\therefore \bar{u} = \frac{1}{2} u_{\max} \quad \text{依題意知 } u = \bar{u}$$

$$\therefore 1 - \frac{r^2}{R^2} = \frac{1}{2}$$

$$\text{解得： } r = 0.707 R$$

即皮托管安設在距管中心 $0.707 R$ 處可直接測得平均流速。

當 $R = \frac{1}{2} d = \frac{1}{2} \times 300 = 150 \text{ mm}$ 時：

$$r = 0.707 \times 150 = 106 \text{ mm}$$

即皮托管應距管中心 106 mm ，距管壁 44 mm 。

當流體在圓管內作湍流流動時：

$$u = u_{\max} \left(1 - \frac{r}{R}\right)^{\frac{1}{7}}$$

$$\therefore \bar{u} = 0.82 u_{\max} \quad \text{且 } u = \bar{u}$$

$$\therefore \left(1 - \frac{r}{R}\right)^{\frac{1}{7}} = 0.82$$



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解得: $r = 0.75 R$
 即皮托管出口在距管中心 $0.75 R$ 處時可直接測得平均流速。
 當 $R = 150 \text{ mm}$ 時, $r = 0.75 \times 150 = 113 \text{ (mm)}$
 故此時皮托管出口距管中心 113 mm , 距管壁 37 mm 。

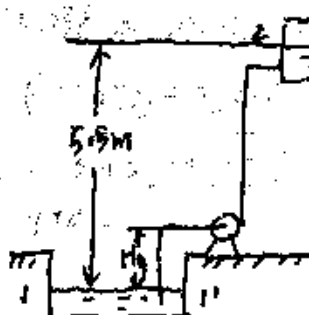
1-23 解: 如圖所示, 在 1、2 截面間列柏努利方程, 并以截面 1 為基準面, 依照意知:

$$Z_1 = 0 \quad Z_2 = 5.5 \text{ m} \quad P_1 = P_a$$

$$P_2 = P_a + 177 \times 10^3$$

$$u_1 = u_2 \approx 0 \quad H_e = H_e$$

$$H_f = H_{f1} + H_{f2} = 1 + 4 = 5 \text{ m}$$



$$\text{据: } Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$$

故系的柏程应为:

$$H_e = 5.5 + \frac{177 \times 10^3}{780 \times 9.81} + 5 = 34.56 \text{ (m)}$$

$$\text{据 } H_g = \frac{P_0 - P_v}{\rho g} - \Delta h - H_{f0-1}$$

故系的名义安装高度应为:

$$H_g = \frac{101325 - 80 \times 10^3}{780 \times 9.81} - 2.6 - 1 = -0.702 \text{ (m)}$$

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若泵位于貯槽液面以下 1.2m 处，低于泵的名义安裝高度，故泵能正常操作。

1-24 解：首先由孔板流量計確定管路中的流量：

$$\text{据 } q_v = C_0 A_0 \sqrt{\frac{2Rg(P' - P)}{\rho}}$$

$$\text{已知 } C_0 = 0.75, A_0 = \frac{\pi}{4} d_0^2 = \frac{\pi}{4} \times 0.038^2 = 0.00113 \text{ (m}^2\text{)}$$

$$R = 0.75 \text{ m } P' = 13600 \text{ Kg/m}^3 \quad \rho = 998.2 \text{ Kg/m}^3 \text{ (20}^\circ\text{C)}$$

$$\therefore q_v = 0.75 \times 0.00113 \times \sqrt{\frac{2 \times 0.75 \times 9.81 \times (13600 - 998.2)}{998.2}}$$

$$= 0.0116 \text{ (m}^3\text{/s)}$$

故吸入管路的流速为：

$$u_\lambda = \frac{4q_v}{\pi d_\lambda^2} = \frac{4 \times 0.0116}{3.14 \times 0.084^2} = 2.1 \text{ (m/s)}$$

在吸入端液面与泵表计处截面之间列柏努利方程，并以吸入端液面为基准面，依题意知：

$$Z_1 = 0, Z_2 = H_g, u_1 \approx 0, u_2 = u_\lambda = 2.1 \text{ m/s } P_1 = P_a$$

$$P_2 = P_a - 7.331 \times 10^4, H_e = 0, H_f = H_{f\lambda}$$

$$\text{据 } Z_1 + \frac{u_1^2}{2g} + \frac{P_1}{\rho g} + H_e = Z_2 + \frac{u_2^2}{2g} + \frac{P_2}{\rho g} + H_f$$

由此可求得安裝高度 H_g 。



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$$\frac{P_a}{\rho g} = H_g + \frac{2.1^2}{2 \times 9.81} + \frac{P_a - 7.33 \times 10^4}{\rho g} + H_{f\lambda}$$

$$H_g = 7.26 - H_{f\lambda}$$

由于在此安装高度下系恰好发生气蚀现象, 故此安装高度应为系的最大安装高度, 即:

$$H_{g\max} = 7.26 - H_{f\lambda}$$

而系的最大安装高度 $H_{g\max}$ 所对应的气蚀厚度为最小气蚀厚度 $\Delta h_{\min}$, 即:

$$H_{g\max} = \frac{P_0 - P_v}{\rho g} - \Delta h_{\min} - H_{f\lambda}$$

$$\text{已知 } P_0 = 1.013 \times 10^5 \text{ Pa} \quad P_v = 2238 \text{ Pa} \quad \rho = 998.2 \text{ kg/m}^3$$

$$\therefore H_{g\max} = \frac{1.013 \times 10^5 - 2238}{998.2 \times 9.81} - \Delta h_{\min} - H_{f\lambda}$$

$$= 10.12 - \Delta h_{\min} - H_{f\lambda}$$

与前列比较后, 允许系的最小气蚀厚度为:

$$\Delta h_{\min} = 10.12 - 7.26 = 2.86 \text{ (m)}$$

其允许气蚀厚度为

$$\Delta h_z = \Delta h_{\min} + 0.3$$

$$= 2.86 + 0.3 = 3.16 \text{ (m)}$$



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1-25 件, 經分析可知該管路為并联管路, 以主管為管路 1, 支管為管路 2, 依題意可知:

$$q_{v2} = 2.72 \text{ m}^3/\text{h} \quad l_1 = 2 \text{ m} \quad l_2 = 10 \text{ m} \quad \lambda_1 = 0.018$$

$$\lambda_2 = 0.03 \quad d_1 = 0.3 \text{ m} \quad d_2 = 0.053 \text{ m}$$

$$\text{據: } \frac{q_{v1}}{q_{v2}} = \sqrt{\frac{d_1^5}{\lambda_1 l_1}} / \sqrt{\frac{d_2^5}{\lambda_2 l_2}}$$

$$= \sqrt{\frac{0.3^5}{0.018 \times 2}} / \sqrt{\frac{0.053^5}{0.03 \times 10}} = 220$$

由此可求得主管(主管路)中的流量為:

$$q_{v1} = 220 q_{v2} = 220 \times 2.72$$

$$= 598.4 (\text{m}^3/\text{h})$$

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$$\frac{P_a}{\rho g} = H_g + \frac{2.1^2}{2 \times 9.81} + \frac{P_a - 7.33 \times 10^4}{\rho g} + H_{f\lambda}$$

$$H_g = 7.26 - H_{f\lambda}$$

由于在此安装高度下系恰好发生气蚀现象，故此安装高度应为系的最大安装高度，即：

$$H_{g\max} = 7.26 - H_{f\lambda}$$

而系的最大安装高度 $H_{g\max}$ 所对应的气蚀厚度为最小气蚀厚度 $\Delta h_{\min}$ ，即：

$$H_{g\max} = \frac{P_0 - P_v}{\rho g} - \Delta h_{\min} - H_{f\lambda}$$

$$\text{已知 } P_0 = 1.013 \times 10^5 \text{ Pa} \quad P_v = 2238 \text{ Pa} \quad \rho = 998.2 \text{ kg/m}^3$$

$$\therefore H_{g\max} = \frac{1.013 \times 10^5 - 2238}{998.2 \times 9.81} - \Delta h_{\min} - H_{f\lambda}$$

$$= 10.12 - \Delta h_{\min} - H_{f\lambda}$$

与前列比较后，允许系的最小气蚀厚度为：

$$\Delta h_{\min} = 10.12 - 7.26 = 2.86 \text{ (m)}$$

其允许气蚀厚度为

$$\Delta h_z = \Delta h_{\min} + 0.3$$

$$= 2.86 + 0.3 = 3.16 \text{ (m)}$$



《化学工程基础》习题参考解答 (温瑞媛)

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第一章 流体的流动与输送

1-1 解: 据 $1 \text{ kgf/cm}^2 = 735.6 \text{ mmHg} = 0.9807 \times 10^5 \text{ Pa}$

已知 $P = 2.5 \text{ kgf/cm}^2$ (表压)

故水银压差计的读数为:

$$R = 2.5 \times 735.6 = 1839 \text{ mmHg (表压)}$$

据: 表压 = 绝压 - 大气压

已知大气压 $P_a = 0.980 \times 10^5 \text{ Pa}$

$$\text{且: } P(\text{表压}) = \frac{1839}{760} \times 101325 = 245180 \text{ Pa}$$

故反应器的真实压强为:

$$P(\text{绝压}) = P_a + P(\text{表压})$$

$$= 0.980 \times 10^5 + 245180 = 3.432 \times 10^5 \text{ Pa}$$

1-2 解: 依题意知油水分离液面内油、水的体积分别为:

$$\text{油: } V_o = \frac{\pi}{4} D^2 h_o$$

$$\text{水: } V_w = \frac{\pi}{4} D^2 h_w$$

$$\text{已知 } V_o/V_w = 5/1$$

$$\therefore \frac{V_o}{V_w} = \frac{\frac{\pi}{4} D^2 h_o}{\frac{\pi}{4} D^2 h_w} = \frac{h_o}{h_w} = \frac{5}{1} \quad \dots\dots (1)$$

液面上压强为:

$$P_{\text{总}} = P_a + \rho_o g h_o + \rho_w g h_w$$



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或 $P_x = P_a + \rho_w g h_c$

$$\therefore \rho_o h_o + \rho_w h_w = \rho_w h_c$$

已知 $\rho_o = 800 \text{ kg/m}^3$ $\rho_w = 1000 \text{ kg/m}^3$ $h_c = 1.1 \text{ m}$

$$\therefore 800 h_o + 1000 h_w = 1.1 \times 1000 \quad \dots\dots (2)$$

聯立(1)、(2)兩式可求得油水面高為：

$$h_w = 0.214 \text{ m}$$

$$\therefore h_o = 5 h_w = 5 \times 0.214 = 1.07 \text{ (m)}$$

故液面總高為：

$$h_w + h_o = 0.214 + 1.07 = 1.284 \text{ (m)}$$

1-37解：(1) 如圖所示，
由於管內水的流速很慢，將其視為
靜止狀態，故有：

$$P_1 = P_2$$

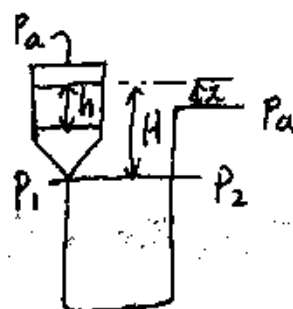
$$\therefore P_1 = P_a + \rho_o g h + (H - h) g \rho_w$$

$$P_2 = P_a + (H - x) g \rho_w$$

$$\therefore x = \frac{\rho_w - \rho_o}{\rho_w} h$$

已知： $\rho_w = 1000 \text{ kg/m}^3$ $\rho_o = 800 \text{ kg/m}^3$ $h = 1 \text{ m}$

$$\therefore x = \frac{1000 - 800}{1000} \times 1 = 0.2 \text{ (m)}$$



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故知結位④ $0 < x < 1m$ 是正確的。

(2) 如圖所示

依然將管內的水處理成靜止狀態。

$$\text{又: } P_0 = P_1, \quad P_2 = P_3$$

$$P_0 = P_a + \rho_w g h$$

$$P_1 = P_2 + \rho_w g h$$

$$P_4 = P_3 + \rho_w g x = P_a$$

$$\therefore h = \frac{\rho_w}{\rho_w - P_0} x$$

$$\text{已知 } x = 0.1m$$

$$\therefore h = \frac{1000}{1000 - 800} \times 0.1 = 0.5(m)$$

1-4 解: 由於空氣的表度極小, 忽略其產生的壓強, 依題意知:

$$P_A = P_a + \rho_{Hg} g R_2 + \rho_{H_2O} g R_3$$

$$\text{已知: } R_2 = 0.045m \quad R_3 = 0.04m$$

$$\therefore P_A = 13600 \times 9.81 \times 0.045 + 1000 \times 9.81 \times 0.04$$

$$= 6396 Pa \text{ (表壓)}$$

$$\text{又: } P_B = P_A + \rho_{Hg} g R_1$$

$$\text{已知: } R_1 = 0.42m$$

$$\therefore P_B = 6396 + 13600 \times 9.81 \times 0.42 = 62431 Pa \text{ (表壓)}$$



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由此可得管头的局部阻力系数:

$$\zeta = \frac{29 H_{f2}}{u^2} = \frac{2 \times 9.81 \times 0.03}{1.17^2} = 0.43$$

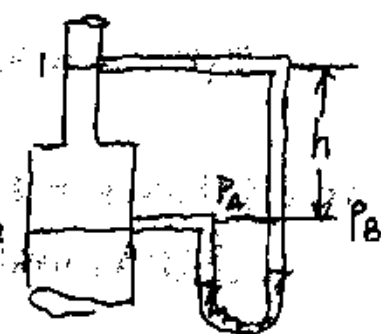
1-2 解: 如图所示

在管路的 1-2 截面之间列伯努利方程, 并以截面 2 为基准面,

依题意知:

$$Z_1 = 1.5 \text{ m}, Z_2 = 0, u_2 = 2.2 \text{ m/s}$$

$$d_1 = 0.1 \text{ m}, d_2 = 0.2 \text{ m}, H_0 = 0$$



$$\text{故: } u_1 = u_2 \left(\frac{d_2}{d_1} \right)^2 = 2.2 \times \left(\frac{0.2}{0.1} \right)^2 = 8.8 \text{ m/s}$$

管路突然扩大, 其阻力系数为:

$$\zeta = \left(1 - \frac{A_1}{A_2} \right)^2 = \left[1 - \left(\frac{d_1}{d_2} \right)^2 \right]^2 = \left[1 - \left(\frac{0.1}{0.2} \right)^2 \right]^2 = 0.5625$$

$$\text{故 } H_f = \zeta \frac{u^2}{2g} = 0.5625 \times \frac{8.8^2}{2 \times 9.81} = 2.22 \text{ (m)}$$

$$\text{根据: } Z_1 + \frac{u_1^2}{2g} + \frac{p_1}{\rho g} + H_0 = Z_2 + \frac{u_2^2}{2g} + \frac{p_2}{\rho g} + H_f$$

$$\text{故: } 1.5 + \frac{8.8^2}{2 \times 9.81} + \frac{p_1}{\rho g} = \frac{2.2^2}{2 \times 9.81} + \frac{p_2}{\rho g} + 2.22$$



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第2章 熱量傳遞習題解答

2-17解: (1) 依題意知 $b_1 = 0.2 \text{ m}$ $b_2 = 0.12 \text{ m}$ $b_3 = 0.006 \text{ m}$

$\lambda_1 = 1.07 \text{ W/m} \cdot ^\circ\text{C}$ $\lambda_2 = 0.15 \text{ W/m} \cdot ^\circ\text{C}$ $\lambda_3 = 45 \text{ W/m} \cdot ^\circ\text{C}$

$t_1 = 1200^\circ\text{C}$ $t_4 = 28^\circ\text{C}$

据: $q = \frac{Q}{S} = \frac{t_1 - t_4}{\frac{b_1}{\lambda_1} + \frac{b_2}{\lambda_2} + \frac{b_3}{\lambda_3}}$

故炉壁的热流密度为:

$$q = \frac{1200 - 28}{\frac{0.2}{1.07} + \frac{0.12}{0.15} + \frac{0.006}{45}} = 1187 \text{ (W/m}^2\text{)}$$

(2) 据 $Q = \frac{\text{总推动力}}{\text{总阻力}} = \frac{\Delta t}{R_{\text{总}}} = \frac{t_1 - t_4}{R_{\text{壁}} + R_{\text{层间}}}$

$$R_{\text{总}} = \frac{t_1 - t_4}{Q_{\text{总}}} = \frac{1200 - 28}{9 \times S} = \frac{1200 - 28}{620 S} = \frac{1.89}{S}$$

$$R_{\text{壁}} = \frac{t_1 - t_4}{Q} = \frac{1200 - 28}{9 S} = \frac{1200 - 28}{1187 S} = \frac{0.987}{S}$$

$$R_{\text{层间}} = R_{\text{总}} - R_{\text{壁}} = \frac{1.89}{S} - \frac{0.987}{S} = \frac{0.903}{S}$$

故层间热阻占总热阻的百分比为:

$$\frac{R_{\text{层间}}}{R_{\text{总}}} = \frac{0.903/S}{1.89/S} = 0.478 = 47.8\%$$

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2-2解: 依題意知 $b_1=0.12\text{m}$ $b_2=0.24\text{m}$ $b_3=0.06\text{m}$
 $\lambda_3=0.2\text{W/m}\cdot^\circ\text{C}$ $t_1=800^\circ\text{C}$ $t_2=680^\circ\text{C}$ $t_3=410^\circ\text{C}$ $t_4=60^\circ\text{C}$

$$\text{据 } q = \frac{t_3 - t_4}{b_3 / \lambda_3}$$

$$\therefore q = \frac{410 - 60}{0.06 / 0.2} = 1166.7 (\text{W/m}^2)$$

$$\therefore \Delta t_1 : \Delta t_2 : \Delta t_3 = R_1 : R_2 : R_3 = \frac{b_1}{\lambda_1} : \frac{b_2}{\lambda_2} : \frac{b_3}{\lambda_3}$$

$$\text{已知 } \Delta t_2 = t_2 - t_3 = 680 - 410 = 270^\circ\text{C}$$

$$\Delta t_3 = t_3 - t_4 = 410 - 60 = 350^\circ\text{C}$$

$$\therefore \frac{0.24 / \lambda_2}{0.06 / 0.2} = \frac{270}{350}$$

$$\text{得 } \lambda_2 = 1.037 (\text{W/m}\cdot^\circ\text{C})$$

$$\text{又 } \Delta t_1 = t_1 - t_2 = 800 - 680 = 120^\circ\text{C}$$

$$\therefore \frac{0.12 / \lambda_1}{0.24 / 1.037} = \frac{120}{270}$$

$$\text{得 } \lambda_1 = 1.167 \text{ W/m}\cdot^\circ\text{C}$$

未加石棉保温层时:

$$q' = \frac{t_1 - t_3}{\frac{b_1}{\lambda_1} + \frac{b_2}{\lambda_2}}$$

$$\text{已知 } t_1 = 800^\circ\text{C} \quad t_3 = 120^\circ\text{C}$$

由此可知其热流密度为:



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$$q' = \frac{800 - 120}{\frac{0.12}{1.167} + \frac{0.24}{1.037}} = 2034.3 \text{ (W/m}^2\text{)}$$

故加石棉层后热损失的减少为:

$$\frac{q' - q''}{q'} = \frac{2034.3 - 1166.7}{2034.3} = 0.426 = 42.6\%$$

2-3 解: 依题意知 $b_1 = b_3 = 0.015 \text{ m}$ $b_2 = b_2$

$$\lambda_1 = \lambda_3 = 0.107 \text{ W/m} \cdot ^\circ\text{C} \quad \lambda_2 = 0.04 \text{ W/m} \cdot ^\circ\text{C} \quad q = 10 \text{ W/m}^2$$

$$t_1 = 21^\circ\text{C} \quad t_4 = -12^\circ\text{C}$$

据 $q = \frac{t_1 - t_4}{\frac{b_1}{\lambda_1} + \frac{b_2}{\lambda_2} + \frac{b_3}{\lambda_3}}$

$$\frac{21 - (-12)}{2 \times \frac{0.015}{0.107} + \frac{b_2}{0.04}} = 10$$

故知软木层的最大厚度为:

$$b_2 = 0.1208 \text{ m}$$

$$\therefore R_{\text{总}} = \frac{b_1}{\lambda_1} + \frac{b_2}{\lambda_2} + \frac{b_3}{\lambda_3} = 2 \times \frac{0.015}{0.107} + \frac{0.1208}{0.04} = 3.3$$

$$R_{\text{软木}} = \frac{b_2}{\lambda_2} = \frac{0.1208}{0.04} = 3.02$$

故软木层的热阻占总热阻的分数为:

$$\frac{R_{\text{软木}}}{R_{\text{总}}} = \frac{3.02}{3.3} = 0.915 = 91.5\%$$



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2-4解: 依題意知 $t_1 = 170^\circ\text{C}$, $t_3 = 30^\circ\text{C}$, $Q/L = 60 \text{ W/m}$
 $r_1 = 0.05 \text{ m}$, $r_2 = 0.1 \text{ m}$, $r_3 = r_3$, $\lambda_1 = 0.06 \text{ W/m}\cdot^\circ\text{C}$, $\lambda_2 = 0.1 \text{ W/m}\cdot^\circ\text{C}$

$$\text{據 } Q = \frac{2\pi L(t_1 - t_3)}{\frac{1}{\lambda_1} \ln \frac{r_3}{r_1} + \frac{1}{\lambda_2} \ln \frac{r_3}{r_2}}$$

$$\frac{2\pi(170 - 30)}{\frac{1}{0.06} \ln \frac{r_3}{0.05} + \frac{1}{0.1} \ln \frac{r_3}{0.1}} = 60$$

可解得: $r_3 = 0.136 \text{ (m)}$

故所包的不帶泥的厚度為:

$$\Delta r_2 = r_3 - r_2 = 0.136 - 0.1 = 0.036 \text{ (m)} = 36 \text{ (mm)}$$

2-5解: 依題意有下列關係:

$$\begin{cases} r_2 - r_1 = r_3 - r_2 \\ r_2 + \frac{r_3 - r_2}{2} = 2 \left(r_1 + \frac{r_2 - r_1}{2} \right) \end{cases}$$

由以上兩式可得:

$$\frac{r_2}{r_1} = 3 \quad \frac{r_3}{r_2} = \frac{5}{3}$$

從內層的導熱係數 $\lambda_1 = \lambda$, 則 $\lambda_2 = 2\lambda$

$$\text{據 } Q = \frac{2\pi L(t_1 - t_3)}{\frac{1}{\lambda_1} \ln \frac{r_3}{r_1} + \frac{1}{\lambda_2} \ln \frac{r_3}{r_2}}$$

則材料位置交換前



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$$Q = \frac{2\pi L(t_1 - t_3)}{\frac{1}{\lambda} \ln 3 + \frac{1}{2\lambda} \ln \frac{5}{3}} = \frac{2\pi L(t_1 - t_3)}{1.354/\lambda}$$

材料的位置互换后:

$$Q' = \frac{2\pi L(t_1 - t_3)}{\frac{1}{2\lambda} \ln 3 + \frac{1}{\lambda} \ln \frac{5}{3}} = \frac{2\pi L(t_1 - t_3)}{1.06/\lambda}$$

故材料互换前后热损失的改变为:

$$\frac{Q'}{Q} = \frac{1.354}{1.06} = 1.28$$

即: $Q' = 1.28Q$

加保温层的作用是减少热损失, 由计算结果可以
看出: 应将保温材料导热系数小, 保温性能好的材
料包在内层(前一种情况), 有利于保温。

所以应包在内层(前一种情况)。

$$Q = \frac{2\pi L(t_1 - t_3)}{\frac{1}{\lambda} \ln 3 + \frac{1}{2\lambda} \ln \frac{5}{3}}$$

$$= \frac{2\pi \times 1 \times (100 - 10)}{\frac{1}{0.024} \ln 3 + \frac{1}{2 \times 0.024} \ln \frac{5}{3}}$$

$$= 340. \dots \text{W/m}^2$$

所以应包在内层(前一种情况)。

$$Q' = \frac{2\pi L(t_1 - t_3)}{\frac{1}{2\lambda} \ln 3 + \frac{1}{\lambda} \ln \frac{5}{3}}$$

$$= \frac{2\pi \times 1 \times (100 - 10)}{\frac{1}{2 \times 0.024} \ln 3 + \frac{1}{0.024} \ln \frac{5}{3}}$$

$$Q' = 435. \dots \text{W/m}^2$$



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2-77 例題已知 $d = 0.021 \text{ m}$, $u = 0.3 \text{ m/s}$
 $\rho = 1230 \text{ kg/m}^3$ $\mu = 4 \times 10^{-3} \text{ Pa}\cdot\text{s}$

$$\therefore Re = \frac{d u \rho}{\mu} = \frac{0.021 \times 0.3 \times 1230}{4 \times 10^{-3}} = 1937 < 2300$$

故流體在圓管內呈強制層流。

又知: $c_p = 2.85 \times 10^3 \text{ J/kg}\cdot^\circ\text{C}$ $\lambda = 0.57 \text{ W/m}\cdot^\circ\text{C}$

$$\therefore Pr = \frac{\mu c_p}{\lambda} = \frac{4 \times 10^{-3} \times 2.85 \times 10^3}{0.57} = 20$$

又 $0.6 < Pr < 6700$

$$\text{而 } \frac{d_i}{L} = \frac{0.021}{3} = 0.007$$

$$\therefore Re \cdot Pr \cdot \frac{d_i}{L} = 1937 \times 20 \times 0.007 = 271.2 > 100$$

因此可用 (2-33) 式求取 α , 即

$$\alpha = 1.86 \frac{\lambda}{d} Re^{1/3} Pr^{1/3} \left(\frac{d_i}{L}\right)^{1/3} \left(\frac{\mu}{\mu_w}\right)^{0.14}$$

$$= 1.86 \times \frac{0.57}{0.021} \times 271.2^{1/3} \times \left(\frac{4 \times 10^{-3}}{3 \times 10^{-3}}\right)^{0.14}$$

$$= 340.2 \text{ (W/m}^2\cdot^\circ\text{C)}$$

設鹽水的出口溫度為 T_2 , 由例 2-6 知:

$$\ln(T_w - T_2) = \ln(T_w - T_1) - \frac{4L\alpha}{d\rho u_b c_p}$$

已知: $T_w = 65^\circ\text{C}$ $T_1 = -5^\circ\text{C}$ $u_b = 0.3 \text{ m/s}$



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$$\therefore \ln(65 - T_2) = \ln[65 - (-5)] - \frac{4 \times 3 \times 340.2}{0.021 \times 1230 \times 0.3 \times 2.85 \times 10^3}$$

解得: $T_2 = 6.82^\circ\text{C}$

2-11 7月: 汽油的质量流量与比热容分别为 g_{mh}, C_{ph} ;
水的质量流量与比热容分别为 g_{mc}, C_{pc} ;

生产任务改变后, 水的出口温度为 t_2 , 由于忽略热损失, 可列出如下热量平衡算式:

任务改变前: $Q = g_{mh} C_{ph} (150 - 100) = g_{mc} C_{pc} (45 - 20)$

任务改变后: $Q' = g_{mh} C_{ph} (150 - 80) = g_{mc} C_{pc} (t_2 - 20)$

由此可解得: $t_2 = 55^\circ\text{C}$

任务改变前的传热温差为:

150	→	100
20	→	45

$\Delta t_1 = 130^\circ\text{C} \quad \Delta t_2 = 55^\circ\text{C}$

$$\therefore \Delta t_m = \frac{\Delta t_1 - \Delta t_2}{\ln \frac{\Delta t_1}{\Delta t_2}} = \frac{130 - 55}{\ln \frac{130}{55}} = 87.2^\circ\text{C}$$

任务改变后的传热温差为:

150	→	80
20	→	55

$\therefore \Delta t'_1 = 130^\circ\text{C} \quad \Delta t'_2 = 25^\circ\text{C}$

$$\therefore \Delta t'_m = \frac{\Delta t'_1 - \Delta t'_2}{\ln \frac{\Delta t'_1}{\Delta t'_2}} = \frac{130 - 25}{\ln \frac{130}{25}} = 63.7^\circ\text{C}$$



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根据传热方程式

$$Q = KA\Delta t_m$$

$$Q' = K'A'\Delta t_m'$$

依题意知: $K = K'$

$$\therefore \frac{Q'}{Q} = \frac{K'A'\Delta t_m'}{KA\Delta t_m} = \frac{A'\Delta t_m'}{A\Delta t_m}$$

$$\text{即: } \frac{q_{mh}C_{ph}(150-80)}{q_{mh}C_{ph}(150-100)} = \frac{63.7A'}{87.2A}$$

$$\therefore \frac{A'}{A} = \frac{\pi d L'}{\pi d L} = 1.916$$

已知: $L = 1.5 \text{ m}$

$$\therefore L' = 1.5 \times 1.916 = 2.874 \text{ (m)}$$

2-12 解: 设重油的流量与比热容分别为 q_{mh} 、 C_{ph} ;

原油的流量与比热容分别为 q_{mc} 、 C_{pc} ;

当为逆流操作时, 重油的出口温度为 T_2 , 原油的出口温度为 t_2 。如换热过程中忽略热损失, 则依题意可对操作改变前后列热量衡算式为:

$$Q = q_{mh}C_{ph}(243-167) = q_{mc}C_{pc}(157-128)$$

$$Q' = q_{mh}C_{ph}(243-T_2) = q_{mc}C_{pc}(t_2-128)$$

化简后得: $T_2 = 578.4 - 2.62t_2$



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逆流操作之传热温差为: $243 \rightarrow 167$
 $128 \rightarrow 157$

$$\therefore \Delta t_1 = 115^\circ\text{C} \quad \Delta t_2 = 10^\circ\text{C}$$

$$\therefore \Delta t_m = \frac{\Delta t_1 - \Delta t_2}{\ln \frac{\Delta t_1}{\Delta t_2}} = \frac{115 - 10}{\ln \frac{115}{10}} = 43^\circ\text{C}$$

逆流操作之传热温差为: $243 \rightarrow 578.4 - 2.62t_2$
 $t_2 \leftarrow 128$

$$\therefore \Delta t_1' = 243 - t_2 \quad \Delta t_2' = 578.4 - 2.62t_2 - 128 = 450.4 - 2.62t_2$$

$$\begin{aligned} \therefore \Delta t_m' &= \frac{\Delta t_1' - \Delta t_2'}{\ln \frac{\Delta t_1'}{\Delta t_2'}} = \frac{243 - t_2 - (450.4 - 2.62t_2)}{\ln \frac{243 - t_2}{450.4 - 2.62t_2}} \\ &= \frac{1.62t_2 - 207.4}{\ln \frac{243 - t_2}{450.4 - 2.62t_2}} \end{aligned}$$

根据传热方程列:

$$Q = KA\Delta t_m$$

$$Q' = K'A'\Delta t_m'$$

依题意知: $K = K' \quad A = A'$

$$\therefore \frac{Q}{Q'} = \frac{\Delta t_m}{\Delta t_m'}$$

$$\text{即: } \frac{9mc C_p (157 - 128)}{9mc C_p (t_2 - 128)} = \frac{43}{\frac{1.62t_2 - 207.4}{\ln \frac{243 - t_2}{450.4 - 2.62t_2}}}$$



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化簡后有

$$1.62t_2 - 207.4 = 1.483(t_2 - 128) \ln \frac{243 - t_2}{450.4 - 2.62t_2}$$

采用試差法求解 t_2 。

當 $t_2 = 161$ 時：左邊 = 53.42 右邊 = 51.56

$t_2 = 162$ 時：左邊 = 55.04 右邊 = 57.4

$t_2 = 161.4$ 時：左邊 = 54 右邊 = 53.8

故知原油的出口溫度 $t_2 = 161.4^\circ\text{C}$

重油的出口溫度為：

$$T_2 = 578.4 - 2.62t_2 = 578.4 - 2.62 \times 161.4 = 155.5^\circ\text{C}$$

243 $\rightarrow$ 155.5

161.4 $\leftarrow$ 128

$\Delta t_1' = 81.6$ $\Delta t_2' = 27.5$

故知逆流操作時的傳熱推動力為

$$\Delta t_m = \frac{\Delta t_1' - \Delta t_2'}{\ln \frac{\Delta t_1'}{\Delta t_2'}} = \frac{81.6 - 27.5}{\ln \frac{81.6}{27.5}} = 49.7^\circ\text{C}$$

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2-13 例：设冷却水的出口温度为 t_2 ，对于逆流操作：

$$\Delta t_1 = 90 - 50 = 40$$

$$t_2 \leftarrow 18$$

$$\Delta t_2 = 50 - 18 = 32^\circ\text{C}$$

$$\therefore \Delta t_m = \frac{\Delta t_1 - \Delta t_2}{\ln \frac{\Delta t_1}{\Delta t_2}} = \frac{40 - 32}{\ln \frac{40}{32}} = \frac{8}{\ln \frac{40}{32}}$$

依题意知换热器所交换的热量为：

$$Q = G_m c_p (T_1 - T_2)$$

$$= \frac{1900}{3600} \times 2.98 \times 10^3 \times (90 - 50) = 6.291 \times 10^4 \text{ (W)}$$

$$\text{已知 } A = 6 \text{ m}^2, K = 230 \text{ W/m}^2 \cdot ^\circ\text{C}$$

$$\text{据 } Q = KA \Delta t_m$$

$$\therefore 230 \times 6 \times \frac{8}{\ln \frac{40}{32}} = 6.291 \times 10^4$$

化简后得：

$$58 - t_2 = 45.6 \ln \frac{40}{32}$$

$$\text{采用试差法：} t_2 = 30 \quad \text{左边} = 28 \quad \text{右边} = 28.7$$

$$t_2 = 27.5 \quad \text{左边} = 30.5 \quad \text{右边} = 30.5$$

故知 $t_2 = 27.5^\circ\text{C}$ (冷却水的出口温度)

冷却水的消耗量为：

$$G_m \times 4.18 \times 10^3 \times (27.5 - 18) = 6.291 \times 10^4$$

$$\therefore G_m = 1.58 \text{ kg/s} = 5.69 \times 10^3 \text{ kg/h}$$



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2-14 附. 依题意知 $\alpha_i = 0.85 \times 10^3$ $\alpha_o = 1.7 \times 10^3$

$\lambda = 45$ $b = 0.0025$ $d_o = 0.025$ $d_i = 0.02$

$$d_m = \frac{d_o - d_i}{\ln \frac{d_o}{d_i}} = \frac{0.025 - 0.02}{\ln \frac{0.025}{0.02}} = 0.0224$$

据 $\frac{1}{K} = \frac{d_o}{\alpha_i d_i} + \frac{b d_o}{\lambda d_m} + \frac{1}{\alpha_o}$

$$\therefore \frac{1}{K} = \frac{0.025}{850 \times 0.02} + \frac{0.0025 \times 0.025}{45 \times 0.0224} + \frac{1}{1700}$$

解得 $K = 471.5 \text{ W/m}^2 \cdot ^\circ\text{C}$

对于逆流操作: $80 \rightarrow 30$

$50 \leftarrow 20$

$$\Delta t_1 = 80 - 50 = 30 \quad \Delta t_2 = 30 - 20 = 10$$

$$\therefore \Delta t_m = \frac{\Delta t_1 - \Delta t_2}{\ln \frac{\Delta t_1}{\Delta t_2}} = \frac{30 - 10}{\ln \frac{30}{10}} = 18.2 (^\circ\text{C})$$

依题意知换热器的热量为:

$$Q = 1.5 \times 1.9 \times 10^3 \times (80 - 30) = 1.425 \times 10^5 \text{ (W)}$$

故冷却水的流量为:

$$q_m \times 4.174 \times 10^3 \times (50 - 20) = 1.425 \times 10^5$$

$$q_m = 1.14 \text{ kg/s}$$

$$S_o = \frac{Q}{K \Delta t_m} = \frac{1.425 \times 10^5}{471.5 \times 18.2} = 16.6 \text{ (m}^2\text{)}$$



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2-15 例. 假设已知操作时的空气温度为:

$$t = \frac{20 + 85}{2} = 52.5^{\circ}\text{C}, \text{查得该温度下空气的物性数据}$$

$$C_p = 1.017 \times 10^3 \text{ J/kg} \cdot ^{\circ}\text{C} \quad \lambda = 2.826 \times 10^{-2} \text{ W/m} \cdot ^{\circ}\text{C}$$

$$\mu = 1.96 \times 10^{-5} \text{ Pa} \cdot \text{s} \quad P_r = 0.698$$

$$\therefore \rho_0 = 1.293 \text{ kg/m}^3 \quad Q_v = 55 \text{ m}^3/\text{h}$$

$$\therefore \rho = \rho_0 \frac{P}{P_0} \frac{T_0}{T} = 1.293 \times \frac{2.026 \times 10^5}{1.013 \times 10^5} \times \frac{273}{325.5} = 2.17 \text{ kg/m}^3$$

$$u = \frac{4Q_v}{\pi d^2} = \frac{4 \times 55}{3600 \times 3.14 \times 0.05^2} = 7.78 (\text{m/s})$$

$$\therefore Re = \frac{du\rho}{\mu} = \frac{0.05 \times 7.78 \times 2.17}{1.96 \times 10^{-5}} = 4.31 \times 10^4 > 10^4$$

$$\therefore L/d_i \geq \frac{3}{0.05} = 60$$

$$\therefore \alpha = 0.023 \frac{\lambda}{d_i} Re^{0.8} P_r^{0.4}$$

空气在管内被加热, 故 $n=0.4$
故空气对管壁的对流传热系数为:

$$\alpha = 0.023 \times \frac{2.826 \times 10^{-2}}{0.05} \times (4.31 \times 10^4)^{0.8} \times 0.698^{0.4}$$

$$= 57.42 (\text{W/m}^2 \cdot ^{\circ}\text{C})$$



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2-16 例：依题意知甲烷气的定性温度为 $t = \frac{120+30}{2} = 75^\circ\text{C}$ ，

查该温度下甲烷气的物性数据为： $\mu = 0.0115 \times 10^{-3} \text{ Pa}\cdot\text{s}$ ，

$\lambda = 0.0407 \text{ W/m}\cdot^\circ\text{C}$ ， $C_p = 2.5 \times 10^3 \text{ J/Kg}\cdot^\circ\text{C}$

甲烷气在壳程内流动时的质量直径为：

$$d_e = 4 \times \frac{\frac{\pi}{4} \times 0.19^2 - \frac{\pi}{4} \times 0.019^2 \times 37}{\pi \times 0.19 + \pi \times 0.019 \times 37} = 0.0255 \text{ (m)}$$

将其视为理想气体，故密度为：

$$\rho = \frac{PM}{RT} = \frac{101325 \times 16 \times 10^{-3}}{8.314 \times 348} = 0.56 \text{ (Kg/m}^3\text{)}$$

已知 $u = 10 \text{ m/s}$

$$Re = \frac{d_e u \rho}{\mu} = \frac{0.0255 \times 10 \times 0.56}{0.0115 \times 10^{-3}} = 12425$$

$$Pr = \frac{C_p \mu}{\lambda} = \frac{2.5 \times 10^3 \times 0.0115 \times 10^{-3}}{0.0407} = 0.706$$

甲烷气在壳程被加热，故 $n = 0.3$

$$\therefore \alpha = 0.023 \frac{\lambda}{d_e} Re^{0.8} Pr^{0.3}$$

$$= 0.023 \times \frac{0.0407}{0.0255} \times 12425^{0.8} \times 0.706^{0.3} = 62.4 \text{ (W/m}^2\cdot^\circ\text{C)}$$

$$\text{据: } \frac{1}{K} = \frac{d_o}{\alpha_i d_i} + \frac{b d_o}{\lambda d_m} + \frac{1}{\alpha_o}$$



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忽略管壁污垢热阻, 且: $d_i = 0.015 \text{ m}$ $d_o = 0.019 \text{ m}$
 $\alpha_i = 850 \text{ W/m}^2 \cdot ^\circ\text{C}$ $\alpha_o = 62.4 \text{ W/m}^2 \cdot ^\circ\text{C}$

$$\therefore \frac{1}{K} = \frac{d_o}{\alpha_i d_i} + \frac{1}{\alpha_o} = \frac{0.019}{850 \times 0.015} + \frac{1}{62.4}$$

由此可求得总传热系数为:

$$K = 57.1 \text{ W/m}^2 \cdot ^\circ\text{C}$$

2-17 解: 设水的流速为 1 m/s 时, 水对管壁传热系数为 α ,

$$\text{据: } \alpha = 0.023 \frac{\lambda}{d} \text{Re}^{0.8} \text{Pr}^n$$

知 $\alpha \propto u^{0.8}$

当水的流速为 1.5 m/s 时, 水对管壁的传热系数为:

$$\alpha' = 1.5^{0.8} \alpha = 1.38 \alpha$$

依题意知 $u = 1 \text{ m/s}$ 时

$$\frac{d_o}{\alpha_i d_i} + \frac{b d_o}{\lambda d_m} + \frac{1}{\alpha_o} = \frac{1}{2115} \quad \dots\dots (1)$$

当 $u = 1.5 \text{ m/s}$ 时:

$$\frac{d_o}{1.38 \alpha_i d_i} + \frac{b d_o}{\lambda d_m} + \frac{1}{\alpha_o} = \frac{1}{2660} \quad \dots\dots (2)$$

$$\therefore d_i = 0.02 \text{ m} \quad d_o = 0.025 \text{ m}$$

$$d_m = \frac{d_o - d_i}{\ln \frac{d_o}{d_i}} = \frac{0.025 - 0.02}{\ln \frac{0.025}{0.02}} = 0.0224 \text{ (m)}$$



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將式(1)、(2)兩式可求得：在 30°C 加 100°C 的 α_0

$$\alpha_0 = 3548.5 \text{ W/m}^2 \cdot ^\circ\text{C}$$

將 α_0 代入到(1)式中可求得蒸氣冷凝的傳熱係數為：

$$\alpha_0 = 35436 \text{ W/m}^2 \cdot ^\circ\text{C}$$

$$\alpha_0 = 35436 \text{ W/m}^2 \cdot ^\circ\text{C}$$

2-187年，在加熱過程某一時刻 $\tau \rightarrow \tau + d\tau$ ，溶液的溫度由 $t \rightarrow t + dt$ ，根據能量衡算可得能量衡算式：

$$KA(T-t)d\tau = G_m C_p dt$$

$$\text{已知 } K = 600 \text{ W/m}^2 \cdot ^\circ\text{C} \quad A = 1 \text{ m}^2 \quad T = 120^\circ\text{C}$$

$$G_m = 1000 \text{ Kg} \quad C_p = 3.8 \times 10^3 \text{ J/Kg} \cdot ^\circ\text{C}$$

$$\therefore 600 \times 1 \times (120-t)d\tau = 1000 \times 3.8 \times 10^3 dt$$

$$\text{故 } d\tau = 6.33 \times 10^3 \times \frac{dt}{120-t}$$

兩邊積分且知邊界條件為： $\tau = 0 \quad t_1 = 25^\circ\text{C}$

及 $\tau = \tau_2 \quad t_2 = 90^\circ\text{C}$

$$\begin{aligned} \therefore \tau &= -6.33 \times 10^3 \ln(120-t) \Big|_{t_1}^{t_2} \\ &= 6.33 \times 10^3 \ln \frac{120-t_1}{120-t_2} = 6.33 \times 10^3 \ln \frac{120-25}{120-90} \\ &= 7.3 \times 10^3 (\text{s}) = 2.03 (\text{h}) \end{aligned}$$

即物料由 25°C 加熱至 90°C 所需時間為 2.03 h。

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2-19 將送熱空氣由 95°C 冷卻至 30°C 放出的熱量為：

$$Q_{\text{放}} = G_m(H_1 - H_2) = 180 \times (11647 - 11467) \times 10^3 \\ = 3.24 \times 10^7 \text{ (J/h)} = 9 \times 10^3 \text{ (W)}$$

30°C 的蒸汽冷凝至 30°C 的液體放出的熱量為：

$$Q_{\text{冷凝}} = 180 \times (11467 - 323) \times 10^3 \\ = 2.059 \times 10^8 \text{ (J/h)} = 5.72 \times 10^4 \text{ (W)}$$

性冷卻水的用量為 G_{mc} ，依題意有：

$$G_{mc} C_{pc} (27 - 15) = 5.72 \times 10^4 + 9 \times 10^3 = 6.62 \times 10^4$$

$$\text{已知 } C_{pc} = 4.183 \times 10^3 \text{ J/kg} \cdot ^{\circ}\text{C}$$

$$\therefore G_{mc} = \frac{6.62 \times 10^4}{4.183 \times 10^3 \times 12} = 1.319 \text{ (kg/s)}$$

設冷卻段與冷凝段交界處水的溫度為 t ，依題意有：

$$1.319 \times 4.183 \times 10^3 \times (t - 15) = 5.72 \times 10^4$$

$$\text{解得： } t = 25.4^{\circ}\text{C}$$

$$\text{對逆流操作： } 15 \rightarrow 25.4 \quad \Delta t_1 = 15$$

$$30 \leftarrow 30 \quad \Delta t_2 = 4.6$$

故冷凝段的平均溫度為：

$$\Delta t_m = \frac{\Delta t_1 - \Delta t_2}{\ln \frac{\Delta t_1}{\Delta t_2}} = \frac{15 - 4.6}{\ln \frac{15}{4.6}} = 8.8 (^{\circ}\text{C})$$

$$\text{對冷卻段： } 25.4 \rightarrow 27 \quad \Delta t'_1 = 6.8$$

$$30 \leftarrow 95 \quad \Delta t'_2 = 4.6$$

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故冷卻段的平均傳熱溫度為

$$\Delta t_m = \frac{\Delta t_1 - \Delta t_2}{\ln \frac{\Delta t_1}{\Delta t_2}} = \frac{68 - 4.6}{\ln \frac{68}{4.6}} = 23.5 (^{\circ}\text{C})$$

2-2 附：若忽略換熱時，設傳熱過程 $\tau \rightarrow \tau + d\tau$ 時刻內，液相的溫度由 $t \rightarrow t + dt$ ，由傳熱速率方程可列出熱量衡算式：

$$KA(T - t) d\tau = G_m C_p dt$$

$$\text{已知：} K = 600 \text{ W/m}^2 \cdot ^{\circ}\text{C} \quad A = 1.2 \text{ m}^2 \quad T = 120 ^{\circ}\text{C}$$

$$G_m = 1000 \text{ Kg} \quad C_p = 3.8 \times 10^3 \text{ J/Kg} \cdot ^{\circ}\text{C}$$

$$\therefore 600 \times 1.2 \times (120 - t) d\tau = 1000 \times 3.8 \times 10^3 dt$$

$$\text{故 } d\tau = 5.28 \times 10^3 \times \frac{dt}{120 - t}$$

$$\text{兩邊積分且知邊界條件為：} \begin{matrix} \tau_1 = 0 & t = 20 ^{\circ}\text{C} \\ \tau_2 = \tau & t = 95 ^{\circ}\text{C} \end{matrix}$$

$$\therefore \tau = -5.28 \times 10^3 \ln(120 - t) \Big|_{t_1}^{t_2}$$

$$= 5.28 \times 10^3 \ln \frac{120 - t_1}{120 - t_2}$$

$$= 5.28 \times 10^3 \ln \frac{120 - 20}{120 - 95}$$

$$= 7.32 \times 10^3 (\text{s}) = 2.03 (\text{h})$$



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若考虑热损失时, 依题意知热量衡算式为:

$$KA(T-t)d\tau - \alpha A_{外表}(t-t_{环境})d\tau = q_m C_p dt$$

$$\text{已知 } \alpha = 8 \text{ W/m}^2 \cdot ^\circ\text{C} \quad A_{外表} = 9.5 \text{ m}^2 \quad t_{环境} = 20^\circ\text{C}$$

$$\therefore 600 \times 1.2 \times (120 - t)d\tau - 8 \times 9.5 \times (t - 20)d\tau = 1000 \times 3.8 \times 10^3 dt$$

化简后: $(87920 - 796t)d\tau = 3.8 \times 10^6 dt$

$$\text{整理: } d\tau = \frac{3.8 \times 10^6}{87920 - 796t} dt$$

$$\text{两边积分且积分边界条件为: } \tau_1 = 0 \quad t_1 = 20$$

$$\tau_2 = \tau \quad t_2 = 95$$

$$\therefore \tau = -\frac{3.8 \times 10^6}{796} \ln \frac{87920 - 796t_2}{87920 - 796t_1}$$

$$= -\frac{3.8 \times 10^6}{796} \ln \frac{87920 - 796 \times 95}{87920 - 796 \times 20}$$

$$= 8.436 \times 10^3 (\text{s}) = 2.34 (\text{h})$$

2-22 解: 依题意知换热过程的传热量为:

$$Q = q_m h r = 0.84 \times 3.56 \times 10^5 = 2.99 \times 10^5 (\text{W})$$

设冷却水的出口温度为 t , 依题意知:

$$19.5 \times 4.174 \times 10^3 \times (t - 32) = 2.99 \times 10^5$$

$$\text{解得: } t = 35.7^\circ\text{C}$$

传热过程的平均温差为:



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$$32 \rightarrow 35.7$$

$$\Delta t_1 = 19.7$$

$$51.7 \rightarrow 51.7$$

$$\Delta t_2 = 16$$

$$\Delta t_m = \frac{\Delta t_1 + \Delta t_2}{2} = \frac{19.7 + 16}{2} = 17.9^\circ\text{C}$$

计算列管内冷却水的传热系数, 按 30°C 查得水的物性数

$$\text{据分别为: } \rho = 995.7 \text{ kg/m}^3 \quad C_p = 4.175 \times 10^3 \text{ J/kg} \cdot ^\circ\text{C}$$

$$\lambda = 0.618 \text{ W/m} \cdot ^\circ\text{C} \quad \mu = 0.801 \times 10^{-3} \text{ Pa} \cdot \text{s}$$

$$Pr = 5.42$$

选择列管内冷却水的流速。据资料 $u = 0.5 \sim 3 \text{ m/s}$ 。因考虑到管外是有机蒸气冷凝, 其传热系数 α 。一般比管内水作强制对流时的传热系数 α_i 大。 α_i 不是主要热阻, 所以 u 不必选得很小, 只要保证 $Re > 10^4$, 这里选 $u = 0.5 \text{ m/s}$ 。

$$\text{已知 } d_i = 0.02 \text{ m}$$

$$\text{则 } Re = \frac{d_i u \rho}{\mu} = \frac{0.02 \times 0.5 \times 995.7}{0.801 \times 10^{-3}}$$

$$= 1.243 \times 10^4 > 10^4$$

$$\text{据: } \alpha = 0.023 \frac{\lambda}{d_i} Re^{0.8} Pr^n$$

列管内冷却水被加热, 故 $n = 0.4$

$$\therefore \alpha_i = 0.023 \times \frac{0.618}{0.02} \times (1.243 \times 10^4)^{0.8} \times 5.42^{0.4}$$

$$= 2631 \text{ (W/m}^2 \cdot ^\circ\text{C)}$$



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第3章 传质分离过程习题解答

3-1 解: 依题意已知 $T_0 = 561 \text{ K}$ $T_2 = 448 \text{ K}$

$$\text{据 } \lg(1.013 \times 10^5) - \lg P_2^* = -\frac{88 T_0}{2.303 R} \left(\frac{1}{T_0} - \frac{1}{T_2} \right)$$

$$\therefore \lg(1.013 \times 10^5) - \lg P_2^* = -\frac{88 \times 561}{2.303 \times 8.314} \left(\frac{1}{561} - \frac{1}{448} \right)$$

$$\text{解得: } P_2^* = 7020 \text{ Pa}$$

$$= 94.280 \text{ Pa (真空度)} = 94.28 \text{ kPa (真空度)}$$

3-2 解: 可用正戊烷和正己烷的沸点平均值取其相对挥发度:

$$\therefore t = \frac{36.1 + 68.7}{2} = 52.4^\circ \text{C}$$

$$\therefore \lg P_1^* = 6.852 - \frac{1065}{52.4 + 232}$$

$$\text{解得: } P_1^* = 1280.2 \text{ mmHg}$$

$$\text{而 } \lg P_2^* = 6.878 - \frac{1172}{52.4 + 224.4}$$

$$\text{解得: } P_2^* = 440.4 \text{ mmHg}$$

$$\therefore \alpha = \frac{P_1^*}{P_2^*} = \frac{1280.2}{440.4} = 2.91$$

由此可知该二元组分溶液的气-液相平衡关系为:



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$$y = \frac{0.2x}{1+(2-1)x} = \frac{2191x}{1+1.91x}$$

3-5 解: 依題意已知 $x_f = 0.84$ $F = 235 \text{ kmol/h}$

$x_d = 0.98$ $x_w = 0.002$

$$\text{据: } \begin{cases} F = D + W \\ Fx_f = Dx_d + Wx_w \end{cases}$$

$$\begin{cases} 235 = D + W \\ 0.84 \times 235 = 0.98D + 0.002W \end{cases}$$

可解得: $D = 201.4 \text{ kmol/h}$ (塔頂采出量)
 $W = 33.6 \text{ kmol/h}$ (塔底采出量)

3-6 解: 依題意已知 $x_f = 0.31$ $F = 8716 \text{ kg/h}$

$x_d = 0.98$ $x_w = 0.012$

$$\text{据: } \begin{cases} F = D + W \\ Fx_f = Dx_d + Wx_w \end{cases}$$

$$\begin{cases} 8716 = D + W \\ 0.31 \times 8716 = 0.98D + 0.012W \end{cases}$$

可解得: $D = 2683.2 \text{ kg/h}$

$W = 6032.8 \text{ kg/h}$

換算成摩爾流量:



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$$D = \frac{2683.2 \times 0.98}{78} + \frac{2683.2 \times 0.02}{92} = 34.3 (\text{Kmol/h})$$

$$W = \frac{6032.8 \times 0.012}{78} + \frac{6032.8 \times 0.988}{92} = 65.7 (\text{Kmol/h})$$

(2) 已知 $R = \frac{L}{D} = 2.5$

故精餾段的回流液量為：

$$L = 2.5D = 2.5 \times 34.3 = 85.75 (\text{Kmol/h})$$

據 $V = L + D$

故精餾段上升的蒸氣量為：

$$V = 85.75 + 34.3 = 120 (\text{Kmol/h})$$

3-7 解：據進料熱狀態參數 q 的定義：

$$q = \frac{\text{氣化 1 mol 料液所需熱量}}{\text{料液沸點氣化焓 } \Delta H_v}$$

$$\therefore q = \frac{1 \times 167.5 \times (94 - 45) + 1 \times 30397.6}{30397.6} = 1.27$$

據 $y = \frac{q}{q-1} x - \frac{1}{q-1} x_f$

已知 $x_f = 0.45$

$$\therefore y = \frac{1.27}{1.27-1} x - \frac{1}{1.27-1} \times 0.45 = 4.7x - 1.67$$



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3-9 解: 先通过气线方程和气-液平衡方程求 x_2, y_2 ;

已知 $\alpha = 2$, 故气-液平衡方程为:

$$y = \frac{\alpha x}{1 + (\alpha - 1)x} = \frac{2x}{1 + x}$$

又气线方程为: $y = 6x - 1.5$

联立以上两式可解得: $x_2 = 0.333$

$$y_2 = 0.5$$

故可求得最小回流比:

$$R_{\min} = \frac{x_d + y_2}{y_2 - x_2} = \frac{0.96 - 0.5}{0.5 - 0.333} = 2.75$$

操作回流比为:

$$R = 1.5 R_{\min} = 1.5 \times 2.75 = 4.13$$

故精馏段的操作线方程为:

$$\begin{aligned} y_{m+1} &= \frac{R}{R+1} x_n + \frac{1}{R+1} x_d = \frac{4.13}{4.13+1} x_n + \frac{1}{4.13+1} \times 0.96 \\ &= 0.805 x_n + 0.187 \end{aligned}$$

(2) 已知 $W = 100 \text{ kmol/h}$ $x_d = 0.96$ $x_w = 0.03$

$$\text{由 } y = \frac{q}{q-1} x - \frac{1}{q-1} x_f = 6x - 1.5$$

可解得: $\begin{cases} q = 1.2 \\ x_f = 0.3 \end{cases}$

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据 $\begin{cases} F = D + W \\ Fx_d = Dx_d + Wx_w \end{cases}$

∴ $\begin{cases} F = D + 100 \\ 0.3F = 0.96D + 0.03 \times 100 \end{cases}$

解得: $D = 40.9 \text{ kmol/h}$ (塔顶产品量)

$F = 140.9 \text{ kmol/h}$ (进料量)

(3) 据 $R' = \frac{x_d - x_w}{x_d - x_f} (R + 1) + 1$

∴ $R' = \frac{0.3 - 0.03}{0.96 - 0.3} (4.13 + 1.2) + 1.2 = 3.38$

据: $y_{m+1} = \frac{R'}{R' - 1} x_m - \frac{1}{R' - 1} x_w$

故精馏段的操作线方程为:

$$\begin{aligned} y_{m+1} &= \frac{3.38}{3.38 - 1} x_m - \frac{1}{3.38 - 1} \times 0.03 \\ &= 1.42 x_m - 0.0126 \end{aligned}$$

3-10 解: 在精馏操作中, 气-液相平衡关系给出的是气-液两相平衡时气相组成 y 与液相组成 x 之间的关系; 而操作线方程给出的是两块塔板气液相组成的关系, 即下一块塔板的气相组成 y 与上一块塔板液相组成 x 的关系。



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3-11 解: 已知 $x_f = 0.4$ $\alpha = 1.5$ $x_d = 0.95$ $q = 1.2$
則 q 線方程為:

$$y = \frac{q}{q-1}x - \frac{1}{q-1}x_f = \frac{1.2}{1.2-1}x - \frac{1}{1.2-1} \times 0.4 \\ = 6x - 2$$

汽液平衡方程為:

$$y = \frac{\alpha x}{1 + (\alpha - 1)x} = \frac{1.5x}{1 + 0.5x}$$

聯立以上兩式可解得: $x_g = 0.42$

$$y_g = 0.52$$

故該精餾過程的最小回流比為:

$$R_{\min} = \frac{x_d - y_g}{y_g - x_g} = \frac{0.95 - 0.52}{0.52 - 0.42} = 4.3$$

3-12 解: 已知 $x_f = 0.835$ $x_d = 0.986$ $x_w = 0.049$
 $\alpha = 1.16$ $q = 1$

$$y_f = \frac{\alpha x_f}{1 + (\alpha - 1)x_f} = \frac{1.16 \times 0.835}{1 + (1.16 - 1) \times 0.835} = 0.854$$

由於是泡點進料, 故最小回流比為:

$$R_{\min} = \frac{x_d - y_f}{y_f - x_f} = \frac{0.986 - 0.854}{0.854 - 0.835} = 6.95$$



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$$\text{据: } n_0 = \frac{\lg \left[\left(\frac{x_d}{1-x_d} \right) \left(\frac{1-x_w}{x_w} \right) \right]}{\lg \alpha} - 1$$

故最小理论塔板数(不包括再沸器)为: $n_0 = 47.6$

$$n_0 = \frac{\lg \left[\left(\frac{0.986}{1-0.986} \right) \left(\frac{1-0.049}{0.049} \right) \right]}{\lg 1.16} - 1 = 47.6$$

3-14 题: 已知 $V=90 \text{ kmol/h}$, $D=30 \text{ kmol/h}$

已知 $x_d=0.95$, $\alpha=2$

$$\text{据 } V=L+D$$

$$L=V-D=90-30=60 \text{ (kmol/h)}$$

$$R = \frac{L}{D} = \frac{60}{30} = 2$$

$$y_{n+1} = \frac{R}{R+1} x_n + \frac{1}{R+1} x_d = \frac{2}{2+1} x_n + \frac{1}{2+1} \times 0.95$$

$$= 0.667 x_n + 0.317$$

$$\therefore y_1 = x_d = 0.95$$

$$\text{则 } y_1 = \frac{0.95}{1+(2-1)x_1} = \frac{2x_1}{1+x_1} = 0.95$$

$$\therefore x_1 = 0.905$$

$$y_2 = 0.667 x_1 + 0.317$$

$$= 0.667 \times 0.905 + 0.317 = 0.92$$



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$$\text{而 } y_2 = \frac{2x_2}{1+x_2} = 0.92$$

故从塔顶数起第二块理论塔板上回流液相的组成为:

$$x_2 = 0.852$$

3-15 解: 用芬斯克公式和吉利兰图求算理论塔板数。

已知: $x_F = 0.3$, $x_d = 0.9$, $x_w = 0.2$, $R = 1.8 R_{\min}$

$$\therefore (T_b)_A = 138.35^\circ\text{C} + 273.15 = 411.5 \text{ K}$$

$$(T_b)_B = 139.1 + 273.15 = 412.25 \text{ K}$$

$$\text{据 } \lg \alpha = -9.178 \left[\frac{(T_b)_A - (T_b)_B}{(T_b)_A + (T_b)_B} \right]$$

$$\therefore \lg \alpha = -9.178 \left[\frac{411.5 - 412.25}{411.5 + 412.25} \right]$$

$$\alpha = 1.02$$

$$\therefore y_f = \frac{\alpha x_f}{1 + (\alpha - 1)x_f} = \frac{1.02 \times 0.3}{1 + (1.02 - 1) \times 0.3} = 0.304$$

由于进料为饱和液体, $q = 1$, 故:

$$R_{\min} = \frac{x_d - y_f}{y_f - x_f} = \frac{0.9 - 0.304}{0.304 - 0.3} = 149$$

$$\therefore R = 1.8 R_{\min} = 1.8 \times 149 = 268.2$$

据芬斯克公式:



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$$n_0 = \frac{\lg \left[\left(1 - \frac{x_d}{1-x_d} \right) \left(\frac{1-x_w}{x_w} \right) \right]}{\lg 2} = 1$$

$$\therefore n_0 = \frac{\lg \left[\left(\frac{0.9}{1-0.1} \right) \times \left(\frac{1-0.2}{0.2} \right) \right]}{\lg 1.02} - 1 = 181$$

$$\frac{R - R_{\min}}{R+1} = \frac{268.2 - 149}{268.2 + 1} = 0.443$$

据此在吉利斯图中可查得:

$$\frac{n_1 - n_0}{n+2} = 0.28$$

由此可知此精馏塔的理论层板数为:

$$N_T = n = 252 \text{ (块)}$$

已知该精馏塔全塔板效率 $E_T = 80\% = 0.8$

$$\text{据 } E_T = \frac{N_T}{N}$$

故该塔的实际塔板数为:

$$N = \frac{N_T}{E_T} = \frac{252}{0.8} = 315 \text{ (块)}$$

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3-16 解: 依题意已知 $x_f = 0.4$ $x_d = 0.95$ $x_w = 0.05$
 $\alpha = 2.41$ $R = 1.2 R_{min}$

$$y_f = \frac{\alpha x_f}{1 + (\alpha - 1)x_f} = \frac{2.41 \times 0.4}{1 + (2.41 - 1) \times 0.4} = 0.616$$

由于为泡点进料, 故:

$$R_{min} = \frac{x_d - y_f}{y_f - x_f} = \frac{0.95 - 0.616}{0.616 - 0.4} = 1.54$$

$$\therefore R = 1.2 R_{min} = 1.2 \times 1.54 = 1.85$$

由此可得精馏段操作线方程为:

$$y_{mi} = \frac{R}{R+1} x_n + \frac{1}{R+1} x_d = \frac{1.85}{1.85+1} x_n + \frac{1}{1.85+1} \times 0.95$$

$$= 0.649 x_n + 0.333$$

气-液平衡线方程为:

$$y = \frac{\alpha x}{1 + (\alpha - 1)x} = \frac{2.41x}{1 + (2.41 - 1)x}$$

可改写为:

$$x = \frac{y}{2.41 - 1.41y}$$

$$\therefore y_1 = x_d = 0.95$$

$$\therefore x_1 = \frac{y_1}{2.41 - 1.41y_1} = \frac{0.95}{2.41 - 1.41 \times 0.95} = 0.887$$



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$$y_2 = 0.649x_1 + 0.333$$

$$= 0.649 \times 0.887 + 0.333 = 0.909$$

依次可计算出精馏段各层板上的汽液组成如表：

	1	2	3	4	5	6	7	8	9
y	0.95	0.909	0.856	0.794	0.733	0.678	0.636	0.606	
x	0.887	0.805	0.711	0.616	0.532	0.466	0.42	0.389	

由于 $x_8 = 0.389 < x_f = 0.4$ ，故第9块塔板在提馏段内，而第8块塔板即为加料板。

$$\text{据 } R' = \frac{x_f - x_w}{x_d - x_f} (R + Q) + Q$$

$$\therefore R' = \frac{0.4 - 0.05}{0.95 - 0.4} \times (1.85 + 1) + 1 = 2.81$$

$$\text{据 } y_{m+1} = \frac{R'}{R' - 1} x_m - \frac{1}{R' - 1} x_w$$

$$\therefore y_{m+1} = \frac{2.81}{2.81 - 1} x_m - \frac{1}{2.81 - 1} \times 0.05$$

$$= 1.55x_m - 0.028$$

$$\therefore y_9 = 1.55x_8 - 0.028$$

$$= 1.55 \times 0.389 - 0.028 = 0.575$$

$$\text{则 } x_9 = \frac{y_9}{2.41 - 1.41y_9} = \frac{0.575}{2.41 - 1.41 \times 0.575} = 0.359$$



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依次可計算出提馏段内初块塔板的气液相组成如表

	9	10	11	12	13	14	15	16	17
y	0.575	0.529	0.465	0.383	0.289	0.196	0.114	0.051	
x	0.359	0.318	0.265	0.205	0.144	0.092	0.051	0.022	

由表中数据可知, 当 $x_b = 0.022 < x_w = 0.05$, 已经能够
满足分离的要求, 因此该塔所需理论板数: $N_T = 16$ 块。

3-18 例: 已知 $x_f = 0.44$ $x_d = 0.97$ $\alpha = 2.5$

据原料为气液混合物, 其中蒸气占 $\frac{1}{3}$ (物质的量之比),
由 q 的定义可知, $q = \frac{2}{3}$ 。

$$\text{据 } y = \frac{q}{q-1}x - \frac{1}{q-1}x_f$$

故加料板上的操作线 (q 线) 方程为:

$$\begin{aligned} y &= \frac{\frac{2}{3}}{\frac{2}{3}-1}x - \frac{1}{\frac{2}{3}-1} \times 0.44 \\ &= 1.32 - 2x \end{aligned}$$

气液平衡线方程为:

$$y = \frac{\alpha x}{1 + (\alpha - 1)x} = \frac{2.5x}{1 + 1.5x}$$

若进料的气-液两相互相平衡, 则 q 线方程与气液
相平衡方程的交点 (x_q, y_q) 即为原料的气液相组成。



聯立兩式可解得:

$$x_2 = 0.365 \text{ (原料中的液相組成)}$$

$$y_2 = 0.59 \text{ (原料中的氣相組成)}$$

$$\text{故 } R_{\min} = \frac{x_d - y_2}{y_2 - x_2}$$

故最小回流比為:

$$R_{\min} = \frac{0.97 - 0.59}{0.59 - 0.365} = 1.69$$

3-19 例. 已知 $x_d = 0.97$ $\alpha = 3$ $R = 2.5$

$$x_1 = 0.5 \quad x_2 = 0.4$$

$$\text{故 } E_{MG} = \frac{y_2 - y_3}{y_2^* - y_3}$$

$$y_2 = \frac{R}{R+1} x_1 + \frac{1}{R+1} x_d = \frac{2.5}{2.5+1} \times 0.5 + \frac{1}{2.5+1} \times 0.97 = 0.634$$

$$y_3 = \frac{R}{R+1} x_2 + \frac{1}{R+1} x_d = \frac{2.5}{2.5+1} \times 0.4 + \frac{1}{2.5+1} \times 0.97 = 0.563$$

$$y_2^* = \frac{\alpha x_2}{1 + (\alpha - 1)x_2} = \frac{3 \times 0.4}{1 + (3-1) \times 0.4} = 0.667$$

$$\therefore E_{MG(2)} = \frac{0.634 - 0.563}{0.667 - 0.563} = 0.683$$



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3-20 解: 已知 $F = 100 \text{ kmol/h}$ $x_f = 0.44$ $x_d = 0.98$

$$x_w = 0.024 \quad R = 3.5$$

据
$$\begin{cases} F = D + W \\ Fx_f = Dx_d + Wx_w \end{cases}$$

$$\therefore \begin{cases} 100 = D + W \\ 100 \times 0.44 = 0.98D + 0.024W \end{cases}$$

可求得: $D = 43.5 \text{ kmol/h}$
 $W = 56.5 \text{ kmol/h}$

$$\therefore R = \frac{L}{D} = 3.5$$

$$\therefore L = 3.5D = 3.5 \times 43.5 = 152.25 \text{ kmol/h}$$

$$\therefore V = L + D$$

$$\therefore V = 152.25 + 43.5 = 195.75 \text{ kmol/h}$$

操作条件为: $p = 101.3 \text{ kPa}$ $T = 273 + 90 = 363 \text{ K}$

故精馏塔内上升蒸汽的体积流量为:

$$q_v = \frac{195.75 \times 10^3}{3600} \times 22.4 \times 10^{-3} \times \frac{363}{273} = 1.62 \text{ (m}^3/\text{s)}$$

已知空塔气速 $u = 0.8 \text{ m/s}$

故此塔的精馏塔径为:

$$d = \sqrt{\frac{4q_v}{\pi u}} = \sqrt{\frac{4 \times 1.62}{3.14 \times 0.8}} = 1.6 \text{ (m)}$$



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3-22 例: 依题意知 $P_A^* = 0.987 \text{ kPa}$ $P_B = 101.3 \text{ kPa}$

$$x_A = \frac{1/17}{1/17 + 100/18} = 0.0105$$

据 $P_A^* = E x_A$

$$\therefore E = \frac{P_A^*}{x_A} = 94 \text{ kPa}$$

据 $m = \frac{E}{P_B}$

故相平衡常数为:

$$m = \frac{94}{101.3} = 0.928$$

据 $H = \frac{P_s}{E M_s}$

已知 $P_s = 998.2 \text{ kg/m}^3$ $M_s = 18 \text{ kg/kmol}$

故溶解度常数为:

$$H = \frac{998.2}{94 \times 18} = 0.59$$



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3-23 例: 依题意已知 $P_A = 21 \text{ kPa}$ $N_A/A = 0.0144 \text{ kmol/m}^2 \cdot \text{h}$

$$C_A = 1 \times 10^{-3} \text{ kmol/m}^3 \quad K_G = 0.0144 \text{ kmol/m}^2 \cdot \text{kPa}$$

$$\text{据 } N_A/A = K_G (P_A - P_{Ai})$$

$$\therefore P_A - P_{Ai} = \frac{N_A/A}{K_G} = \frac{0.0144}{0.0144} = 10 \text{ (kPa)}$$

$$\text{据 } P_A^* = \frac{C_A}{H}$$

$$\text{当 } P_A^* = 8 \text{ kPa 时, } C_A = 1 \times 10^{-3} \text{ kmol/m}^3$$

$$\therefore H = \frac{C_A}{P_A^*} = \frac{1 \times 10^{-3}}{8} = 1.25 \times 10^{-4} \text{ (kmol/m}^3 \cdot \text{kPa)}$$

$$\text{据 } N_A/A = K_G (P_A - P_A^*)$$

$$\therefore K_G = \frac{N_A/A}{P_A - P_A^*} = \frac{0.0144}{21 - 8} = 0.0111$$

$$\text{据 } \frac{1}{K_G} = \frac{1}{K_G} + \frac{1}{HK_L}$$

$$\therefore \frac{1}{0.0111} = \frac{1}{0.0144} + \frac{1}{1.25 \times 10^{-4} K_L}$$

$$\text{求得: } K_L = 384 \text{ m/h}$$

$$\text{据 } \frac{1}{K_L} = \frac{H}{K_G} + \frac{1}{K_L}$$

$$\therefore \frac{1}{K_L} = \frac{1.25 \times 10^{-4}}{0.0144} + \frac{1}{384}$$



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求得: $K_L = 88.6 \text{ m/h}$

据: $N_A/A = K_L(C_A^* - C_A)$

$$\therefore C_A^* - C_A = \frac{N_A/A}{K_L} = \frac{0.144}{88.6} = 1.625 \times 10^{-3} (\text{kmol/m}^3)$$

总阻力为 $1/K_G$, 气膜阻力为 $1/K_G$

故气膜阻力占总阻力的百分率为:

$$\frac{1/K_G}{1/K_G} = \frac{K_G}{K_G} = \frac{0.0111}{0.0144} = 0.77 = 77\%$$

3-24 题: 已知 $k_G = 0.003 \text{ kmol/h} \cdot \text{m}^2 \cdot \text{kPa}$ $k_L = 0.45 \text{ m/h}$

$$P_{\text{总}} = 106.4 \text{ kPa} \quad Y = 320 \text{ mmHg}$$

由 $Y = 320 \text{ mmHg}$ 可知 $m = 320$

$$\text{据 } m = \frac{E}{P_{\text{总}}}$$

$$\therefore E = m P_{\text{总}} = 320 \times 106.4 = 34048 \text{ kPa}$$

$$\text{据 } H = \frac{P_s}{E M_s}$$

$$\text{已知 } P_s = 1000 \text{ kg/m}^3 \quad M_s = 18 \text{ kg/kmol}$$

$$\therefore H = \frac{1000}{34048 \times 18} = 1.631 \times 10^{-3} (\text{kmol/m}^3 \cdot \text{kPa})$$

$$\text{据 } \frac{1}{K_G} = \frac{1}{k_G} + \frac{1}{H k_L}$$



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$$\therefore \frac{1}{K_G} = \frac{1}{0.003} + \frac{1}{1.631 \times 10^{-3} \times 0.45}$$

$$\therefore K_G = 5.9 \times 10^{-4} \text{ kmol/h} \cdot \text{m}^2 \cdot \text{kPa}$$

据 $K_G = H K_L$

$$\therefore K_L = \frac{K_G}{H} = \frac{5.9 \times 10^{-4}}{1.631 \times 10^{-3}} = 0.362$$

据 $K_y = P_m K_G$

$$\therefore K_y = 106.4 \times 5.9 \times 10^{-4} = 6.28 \times 10^{-2} \text{ (kmol/h} \cdot \text{m}^2 \cdot \text{kPa)}$$

据 $K_x = C_m K_L$

而 $C_m \approx \frac{P_s}{M_s}$

$$\therefore K_x = \frac{1000}{18} \times 0.362 = 20.1 \text{ (kmol/h} \cdot \text{m}^2 \cdot \text{kPa)}$$

3-25 题: 120 题已知 $y_1 = 0.02$, $y_2 = 0.001$, $E = 5.52 \times 10^4 \text{ kPa}$
 $P_m = 101.3 \text{ kPa}$, $x_2 = 0$ (清水)

$$\therefore Y_1 = \frac{y_1}{1-y_1} = \frac{0.02}{1-0.02} = 0.0204$$

$$Y_2 = \frac{y_2}{1-y_2} = \frac{0.001}{1-0.001} = 0.001$$

$$m = \frac{E}{P_m} = \frac{5.52 \times 10^4}{101.3} = 545$$



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$$\text{根据 } \left(\frac{L}{V}\right)_{\min} = \frac{Y_1 - Y_2}{\frac{Y_1}{m} - X_2}$$

$$\therefore \left(\frac{L}{V}\right)_{\min} = \frac{0.0204 - 0.001}{\frac{0.0204}{54.5} - 0} = 518.3$$

$$\therefore L = 1.2 L_{\min}$$

$$\therefore \left(\frac{L}{V}\right) = 1.2 \left(\frac{L}{V}\right)_{\min} = 1.2 \times 518.3 = 622$$

$$\text{根据 } \frac{L}{V} = \frac{Y_1 - Y_2}{X_1 - X_2}$$

$$\text{则 } \frac{0.0204 - 0.001}{X_1 - 0} = 622$$

$$\therefore X_1 = 3.12 \times 10^{-5}$$

若操作压强改为 1013 kPa, 即 $P_A' = 1013 \text{ kPa}$

$$\text{则 } m' = \frac{5.52 \times 10^4}{1013} = 54.5$$

$$\therefore \left(\frac{L}{V}\right)'_{\min} = \frac{0.0204 - 0.001}{\frac{0.0204}{54.5} - 0} = 51.83$$

$$\left(\frac{L}{V}\right)' = 1.2 \times 51.83 = 62.2$$

$$\text{则 } \frac{0.0204 - 0.001}{X_1' - 0} = 62.2$$

$$\therefore X_1' = 3.12 \times 10^{-4}$$



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3-26.44. 已知 $H=6$ $m=2$ $y_1=0.05$ $z_2=0$ (清水)

$$y_2 = Y_2 = 0.00263$$

$$X.1: Y_1 = \frac{y_1}{1-y_1} = \frac{0.05}{1-0.05} = 0.0526$$

依题意可知

$$Z_1 = \frac{6.12/58}{93.88/18} = 0.0202$$

$$\therefore Y_1^* = m Z_1 = 2 \times 0.0202 = 0.0404$$

$$Y_2^* = m Z_2 = 0$$

$$\Delta Y_1 = Y_1 - Y_1^* = 0.0526 - 0.0404 = 0.0122$$

$$\Delta Y_2 = Y_2 - Y_2^* = 0.00263$$

$$\Delta Y_m = \frac{\Delta Y_1 - \Delta Y_2}{\ln \frac{\Delta Y_1}{\Delta Y_2}} = \frac{0.0122 - 0.00263}{\ln \frac{0.0122}{0.00263}} = 0.0062$$

$$N_{OG} = \frac{Y_1 - Y_2}{\Delta Y_m} = \frac{0.0526 - 0.00263}{0.0062} = 8$$

依题意知

$$V = \frac{2000}{22.4} \times \frac{273}{298} \times (1-0.05) = 77.7 \text{ (kmol/h)}$$

$$\Omega = \frac{\pi}{4} d^2 = \frac{\pi}{4} \times 0.8^2 = 0.5024 \text{ (m}^2\text{)}$$

$$\text{据 } H = H_{OG} \times N_{OG} = \frac{V}{K_y a \Omega} \times N_{OG}$$



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故气相体积总传质系数为:

$$K_{ya} = \frac{V N_{O_2}}{A \Delta} = \frac{77.7 \times 8}{6 \times 0.5024} = 206.2 \text{ (Kmol/h} \cdot \text{m}^3 \cdot \text{h)}$$

据 $N = V(Y_1 - Y_2)$

故每小时回收的丙酮量为:

$$N = 77.7 \times (0.0526 - 0.00263) = 3.88 \text{ (Kmol/h)}$$

3-27 解: 已知 $y_1 = 0.1$ $y_2 = 0.005$ $x_1 = 0.0006$ $x_2 = 0$
 $E = 2 \times 10^5 \text{ KPa}$ $P_{\text{总}} = 2 \times 10^3 \text{ KPa}$

$$Y_1 = \frac{y_1}{1-y_1} = \frac{0.1}{1-0.1} = 0.111$$

$$Y_2 = \frac{y_2}{1-y_2} = \frac{0.005}{1-0.005} = 0.005$$

$$x_1 \approx x_1 = 0.0006$$

$$m = \frac{E}{P_{\text{总}}} = \frac{2 \times 10^5}{2 \times 10^3} = 100$$

$$\therefore \frac{L}{V} = \frac{Y_1 - Y_2}{x_1 - x_2} = \frac{0.111 - 0.005}{0.0006 - 0} = 176.67$$

依题意可知: $V = \frac{2240}{22.4} \times (1-0.1) = 90 \text{ (Kmol/h)}$

故每小时回收量为:

$$L = 176.67 \times 90 = 15900 \text{ (Kmol/h)} = 286200 \text{ kg/h} = 286.2 \text{ t/h}$$



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$$\therefore \bar{x}_1^* = \frac{Y_1}{m} = \frac{0.111}{100} = 0.00111$$

$$\bar{x}_2^* = \frac{Y_2}{m} = \frac{0.005}{100} = 0.00005$$

$$\Delta \bar{x}_1 = \bar{x}_1^* - \bar{x}_1 = 0.00111 - 0.0006 = 0.00051$$

$$\Delta \bar{x}_2 = \bar{x}_2^* - \bar{x}_2 = 0.00005$$

$$\Delta \bar{x}_m = \frac{\Delta \bar{x}_1 - \Delta \bar{x}_2}{\ln \frac{\Delta \bar{x}_1}{\Delta \bar{x}_2}} = \frac{0.00051 - 0.00005}{\ln \frac{0.00051}{0.00005}} = 0.000198$$

$$\therefore N_{OL} = \frac{\bar{x}_1 - \bar{x}_2}{\Delta \bar{x}_m} = \frac{0.0006 - 0}{0.000198} = 3.03$$

依题意已知 $K_L a = 2780 \text{ kmol/h} \cdot \text{m}^3$

$$\Omega = \frac{\pi}{4} d^2 = \frac{\pi}{4} \times 1.5^2 = 1.766 \text{ (m}^2\text{)}$$

$$\therefore H_{OL} = \frac{L}{K_L a \Omega} = \frac{15900}{2780 \times 1.766} = 3.24 \text{ (m)}$$

故填料层的高度为：

$$H = H_{OL} \times N_{OL} = 3.24 \times 3.03 = 9.81 \text{ (m)}$$